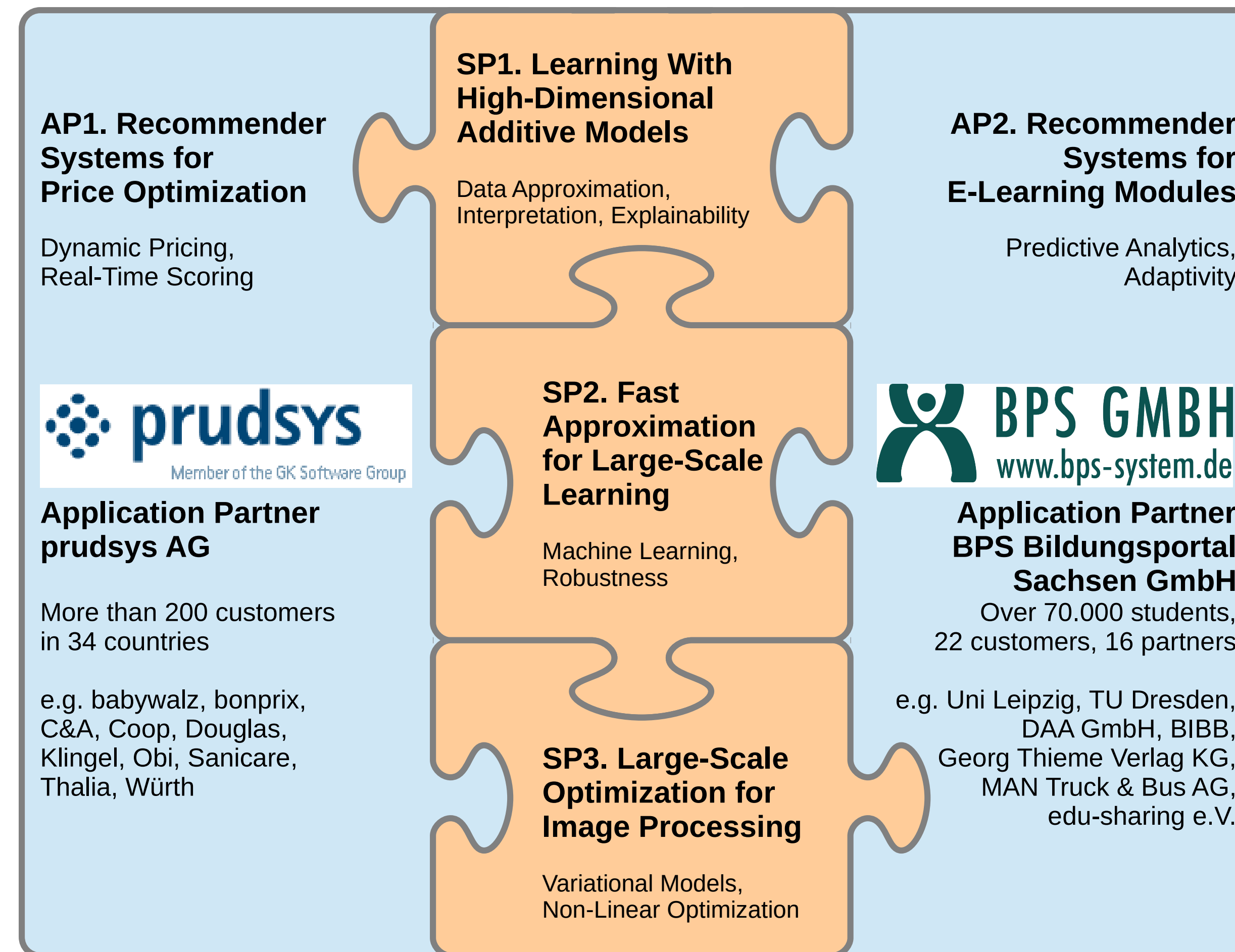


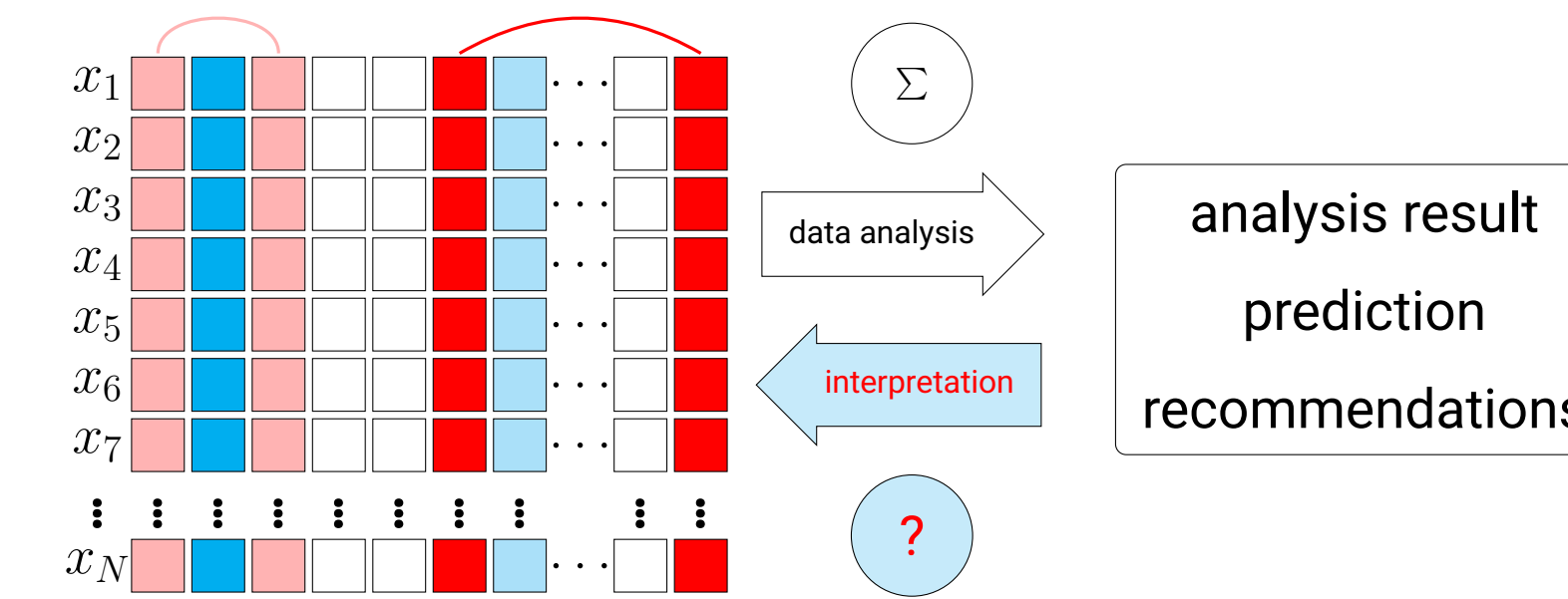
SALE



ger.: **S**chnelle **A**lgorithmen für transparente **E**mpehlungssysteme

Idea and goals of the project

- As the storage of data increases, so do the requirements placed on processes for their meaningful and, above all, transparent analysis.
- Goal of this project: Develop efficient algorithms for data analysis, which allow **conclusions to be drawn about the decision-making process** (explainable AI).



- The focus is particularly on methods related to the **analysis of variance (ANOVA)**.
- Based on the **ANOVA decomposition** of a function

$$f(\mathbf{x}) = f_0 + \sum_{i=1}^d f_{\{i\}}(\mathbf{x}) + \sum_{i,j=1,i<j}^d f_{\{i,j\}}(\mathbf{x}) + \dots + f_{\{1,2,\dots,d\}}(\mathbf{x})$$

interactions between dimensions can be analyzed.

- We assume a **sparsity**, which is given in many practical applications (sparsity of effects).
- Sensitivity analysis:** The global sensitivity indices (gsi) indicate which dimensional couplings are important in the data.

Example (function in 9D):

$$f(x_1, \dots, x_9) = u(x_1, x_3, x_8) + v(x_2, x_5, x_6) + w(x_4, x_7, x_9)$$

with active set $\mathcal{A} = \mathcal{P}(\{1, 3, 8\}) \cup \mathcal{P}(\{2, 5, 6\}) \cup \mathcal{P}(\{4, 7, 9\})$

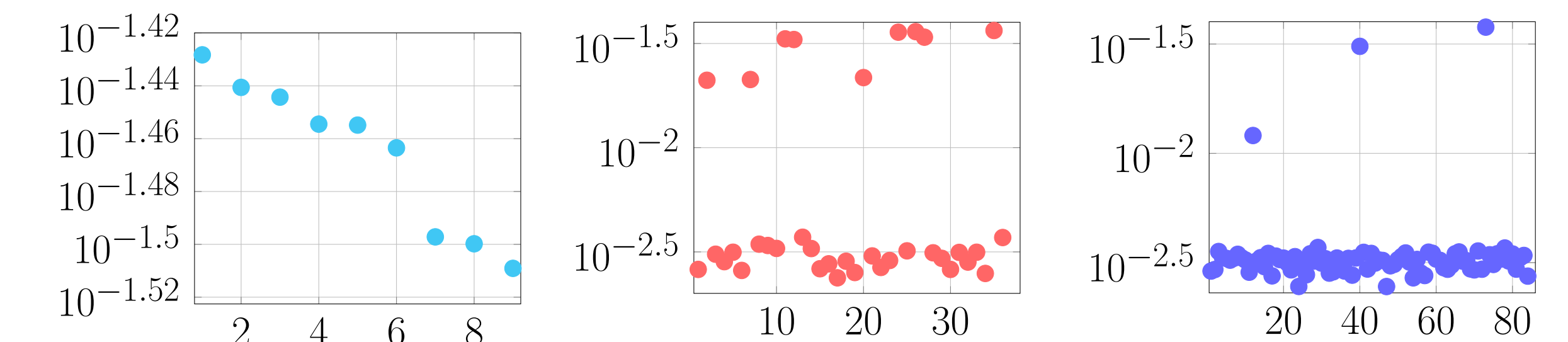
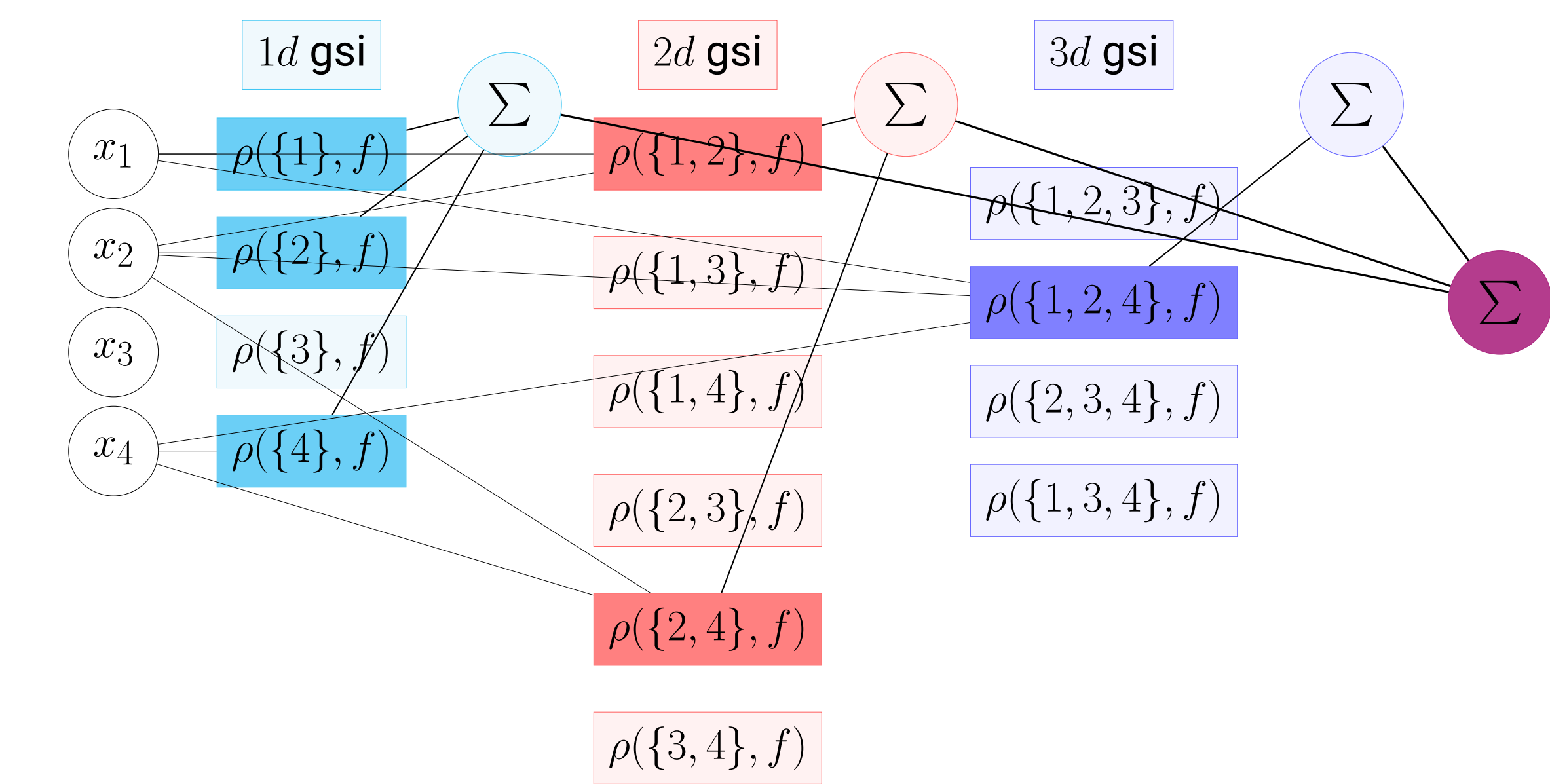


Figure: Approximation problem in 9D, influence (gsi) of single dimensions and their interactions.

An explainable ANOVA network:



Subproject 1

Learning With High-Dimensional Additive Models

- Cooperation with the chair for applied functional analysis, Prof. Daniel Potts (TU Chemnitz)
- Fast Algorithms for high-dimensional approximation
- FFT-based methods
- Interpretability based on the ANOVA decomposition in Fourier domain

Subproject 2

Fast Approximation for Large-Scale Learning

- Cooperation with the chair for scientific computing, Prof. Martin Stoll (TU Chemnitz)
- Machine learning, fast methods for matrix-vector multiplication
- Kernel based methods (ridge regression, SVM, spectral clustering)
- Interpretability via ANOVA kernels

Subproject 3

Large-Scale Optimization for Image Processing

- Cooperation with the chair for applied mathematics, Prof. Gabriele Steidl (TU Berlin)
- Variational models, non-linear optimization
- Optimization and mixture models
- Interpretability based on sparse mixture models

People



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Head of project



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Publications

F. Nestler, M. Stoll, T. Wagner: **Learning in High-Dimensional Feature Spaces Using ANOVA-Based Fast Matrix-Vector Multiplication**. arXiv: 2111.10140, 2021.

D. Potts, M. Schmischke: **Interpretable Transformed ANOVA Approximation on the Example of the Prevention of Forest Fires**. arXiv: 2110.07353, 2021.

J. Hertrich, F. A. Ba, G. Steidl: **Sparse Mixture Models Inspired by ANOVA Decompositions**. Electronic Transactions on Numerical Analysis, vol. 55, pp. 142–168, 2021.

D. Potts, M. Schmischke: **Interpretable Approximation of High-Dimensional Data**. SIAM Journal on Mathematics of Data Science, 3 (4), 1301–1323, 2021.

Software

D. Potts, M. Schmischke: <https://github.com/NFFT/ANOVAapprox.jl> (Julia)

F. Bartel, D. Potts, M. Schmischke: <https://github.com/NFFT/GroupedTransforms.jl> (Julia)

F. Nestler, M. Stoll, T. Wagner: <https://github.com/wagnertheresa/NFFT4ANOVA> (Python)