

Discretization of Control Constrained Optimal Control Problems with Mass Lumping

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In this talk we consider the optimal control of an elliptic PDE subject to pointwise control constraints. We discretize the problem with higher order finite elements in order to achieve fast convergence with respect to the mesh width h .

We propose a discretization of the optimal control problem which uses lumping for the mass matrices. This scheme has the advantage that “optimization” and “discretization” commute. We provide a-priori error estimates. In the case of P^2 finite elements, we achieve the order h^2 for the L^2 error in the state and the adjoint state on polygonal convex domains. We also obtain convergence order h^2 for the optimal control in the nodes of the discretization and for a post-processed control. The order can be improved to h_{global}^3 by a local refinement at the boundary of the active set.

The theoretical findings are confirmed by numerical experiments.

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