Counting rainbow colorings

MARKUS DOD ‡, SARA KISCHNICK^{*}, PETER TITTMANN^{*} ‡IVM Institut für Vernetzte Mobilität gGmbH ^{*} University of Applied Sciences Mittweida

A rainbow coloring of an undirected graph G is an edge coloring such that every pair of vertices is connected by a path for which no two edges are colored alike. The rainbow polynomial $\rho(G, x)$ counts the number of rainbow colorings of the graph G with x colors. An s-rainbow coloring is an edge coloring of G such that there exist rainbow paths from an arbitrary vertex s to all other vertices of G. We define the s-rainbow polynomial $\rho(G; s, x)$ and present some results for this polynomial.