



Dynamic Covariance Scaling for Robust Robot Mapping

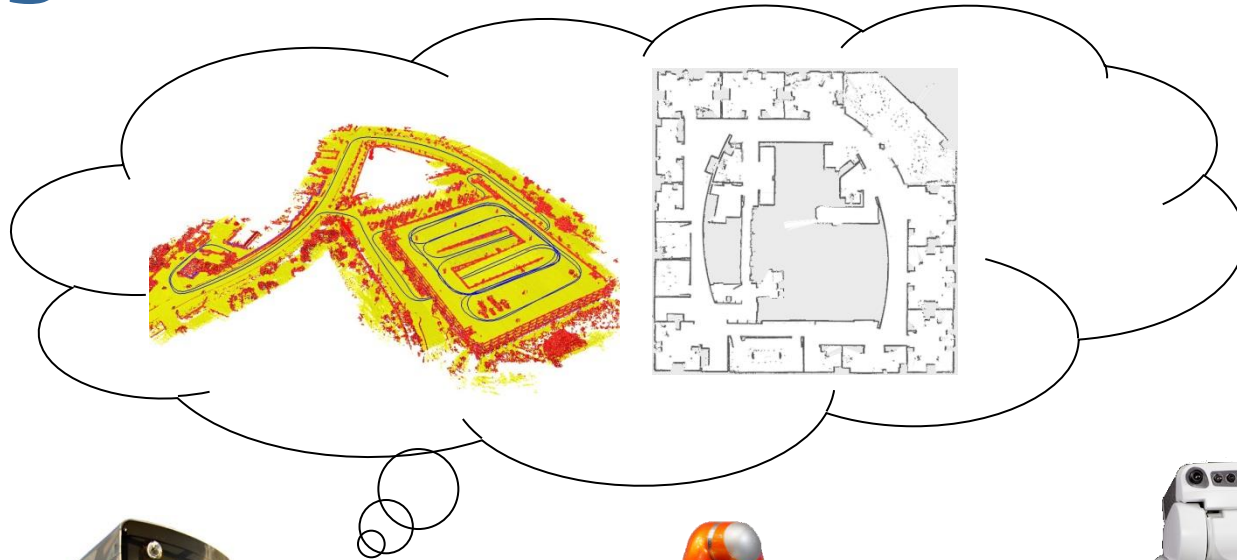
**Workshop on Robust and
Multimodal Inference in Factor Graphs**



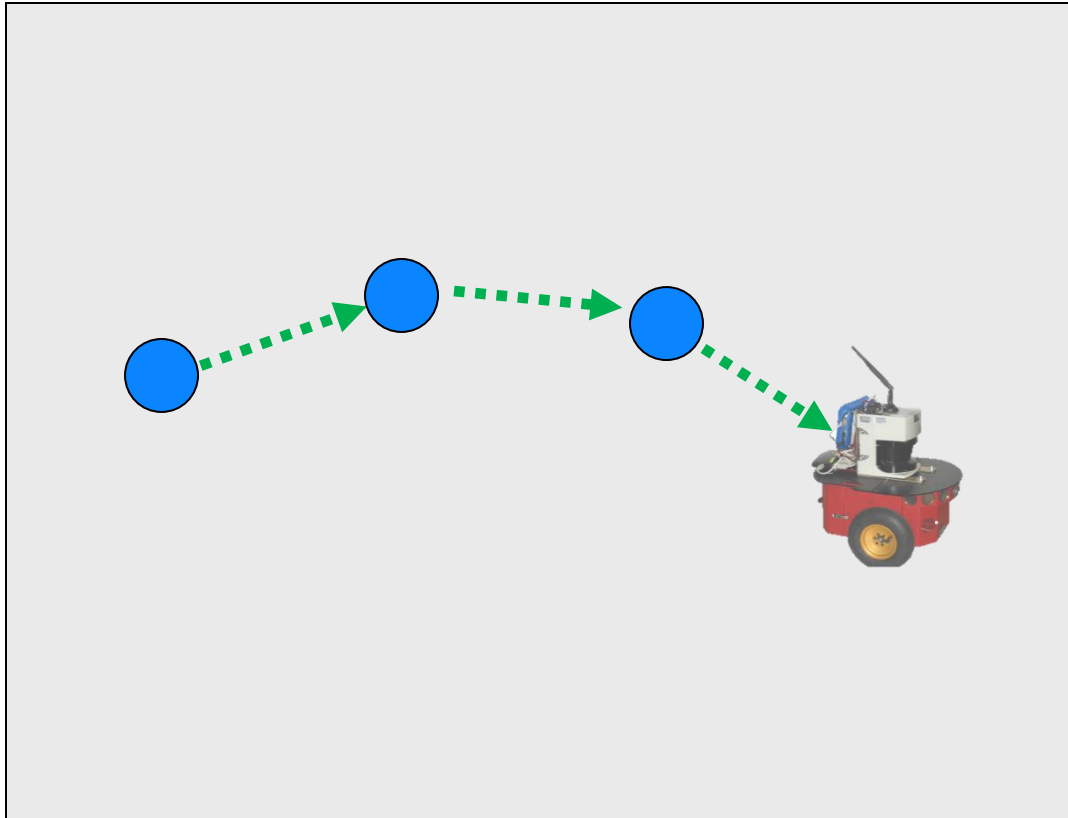
Pratik Agarwal, Gian Diego Tipaldi, Luciano Spinello,
Cyrill Stachniss and Wolfram Burgard

University of Freiburg, Germany

Maps are Essential for Effective Navigation



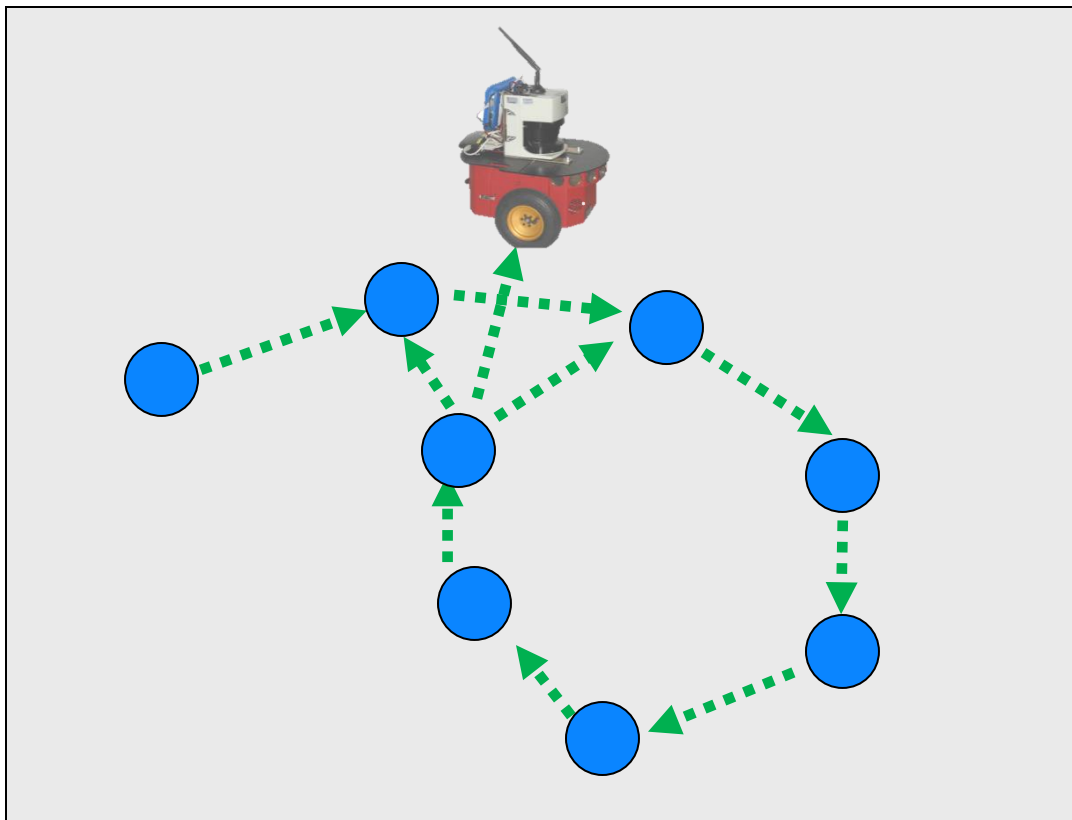
Graph-based SLAM



● Robot pose

→ Constraint

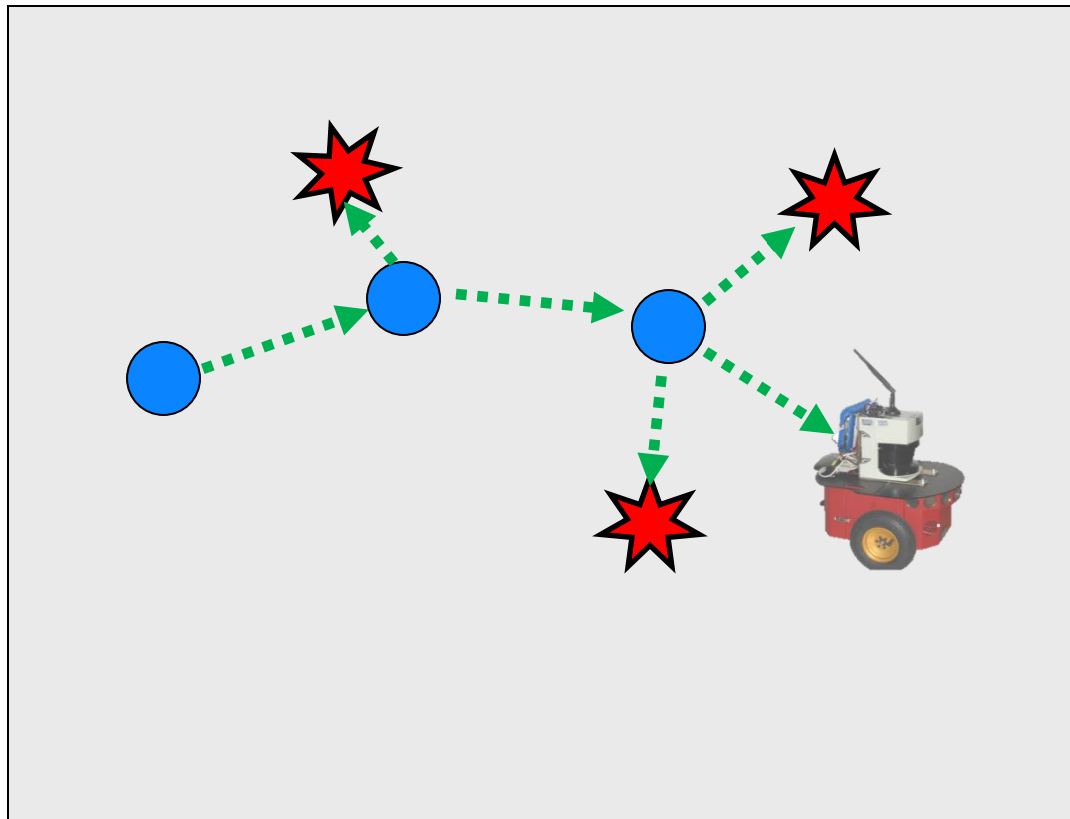
Graph-based SLAM



 Robot pose

 Constraint

Graph-based SLAM

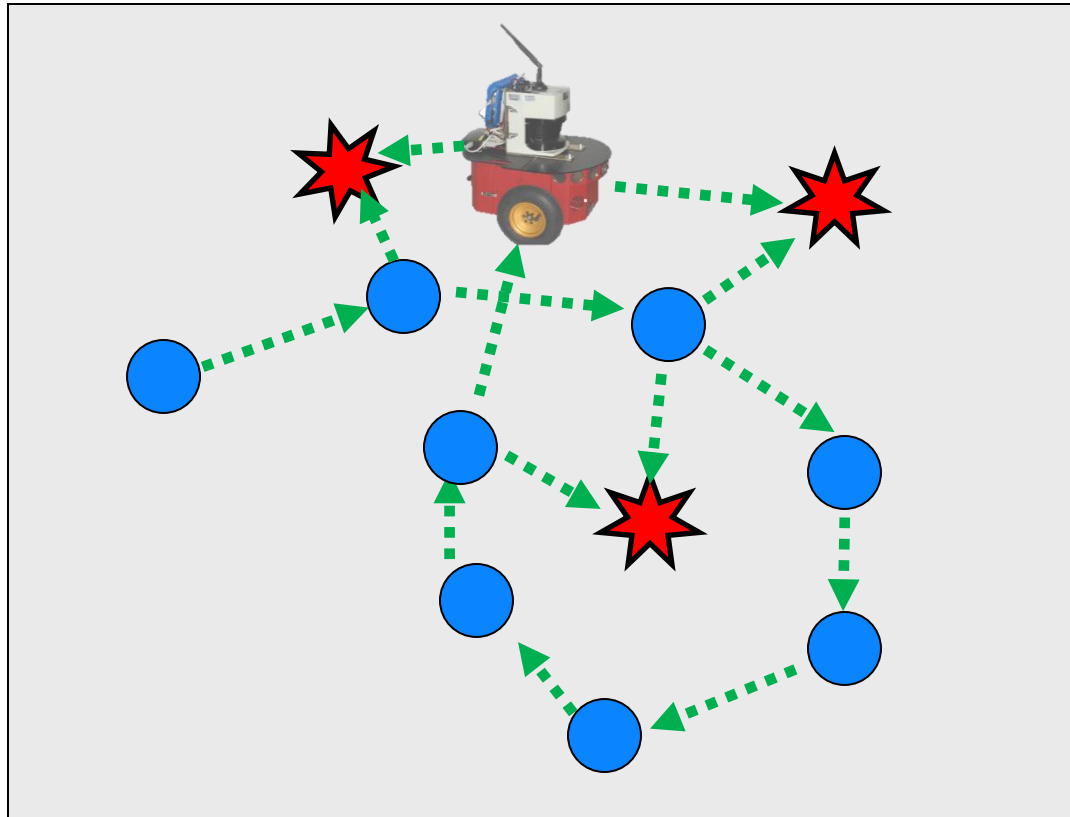


● Robot pose

→ Constraint

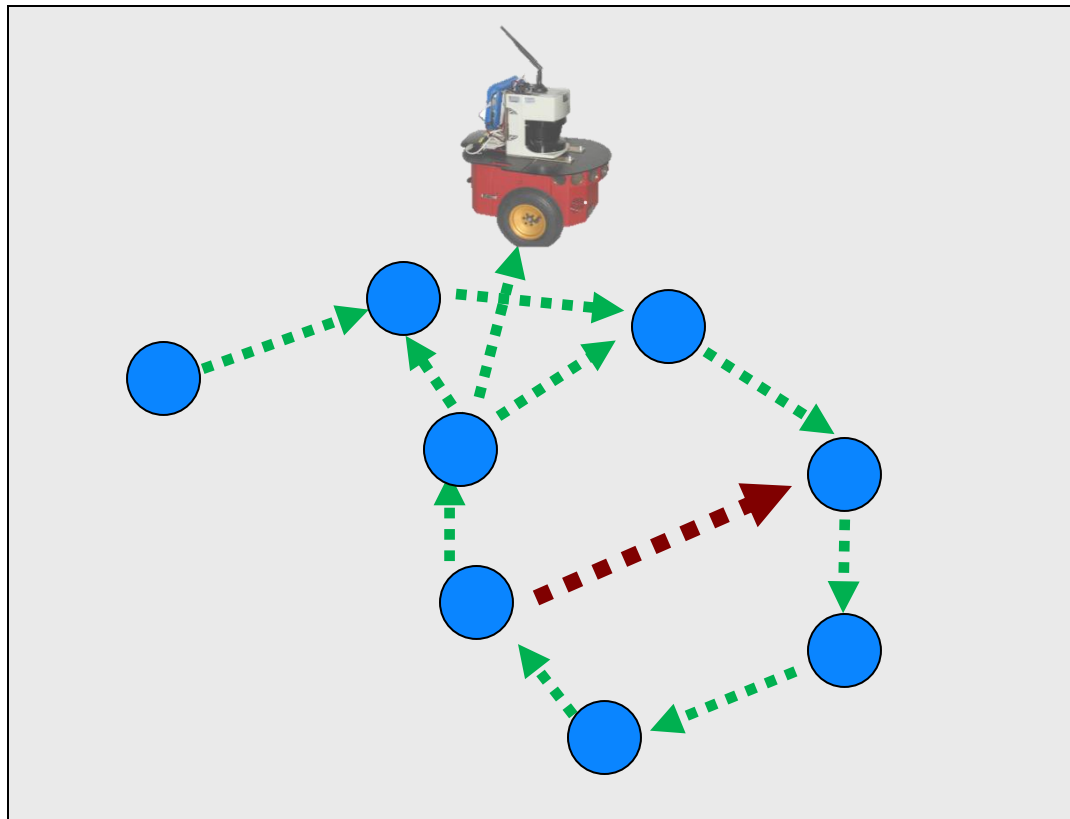
★ Landmark

Graph-based SLAM



- Robot pose
- Constraint
- ★ Landmark

Graph-based SLAM

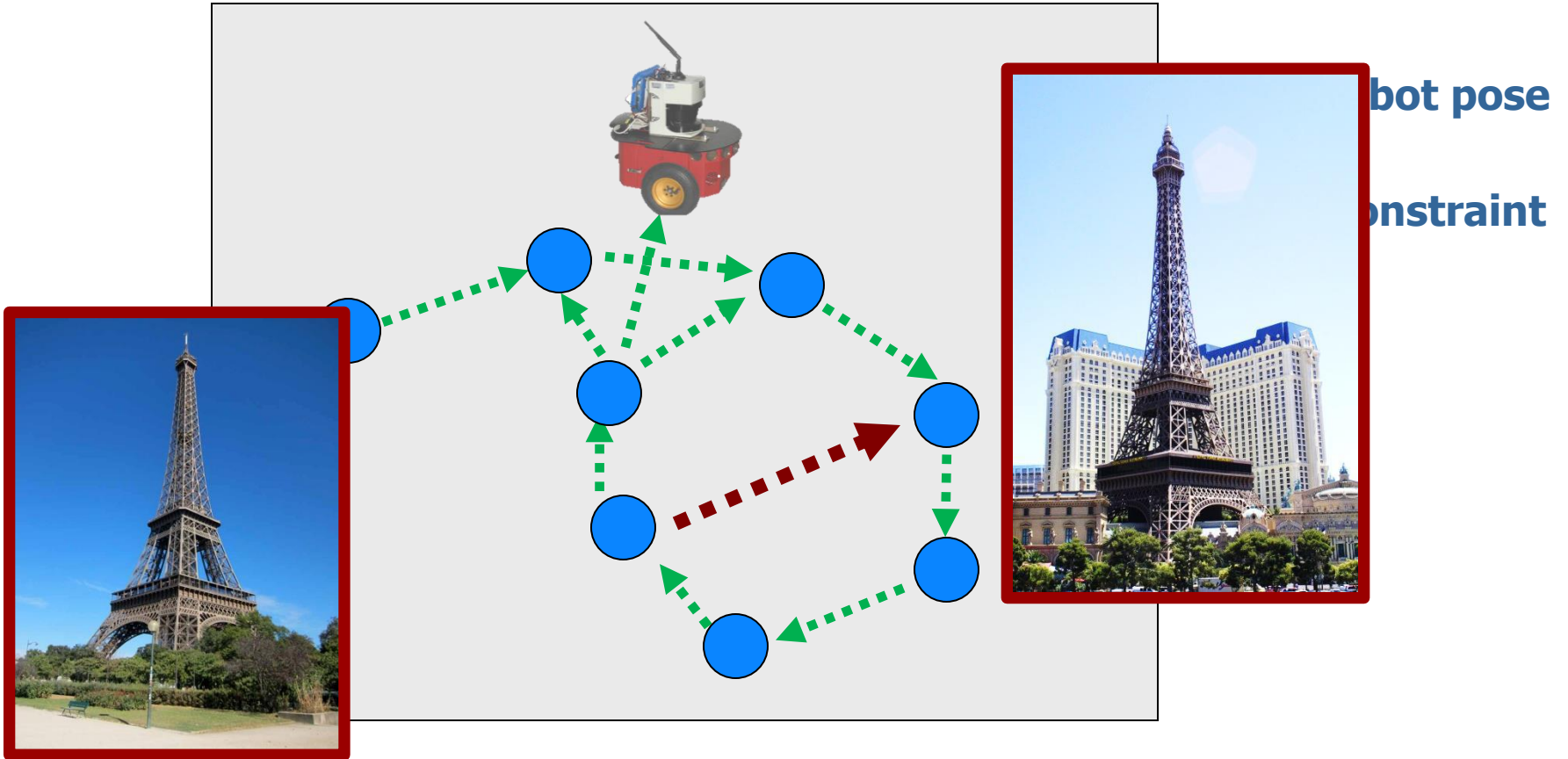


● Robot pose

→ Constraint

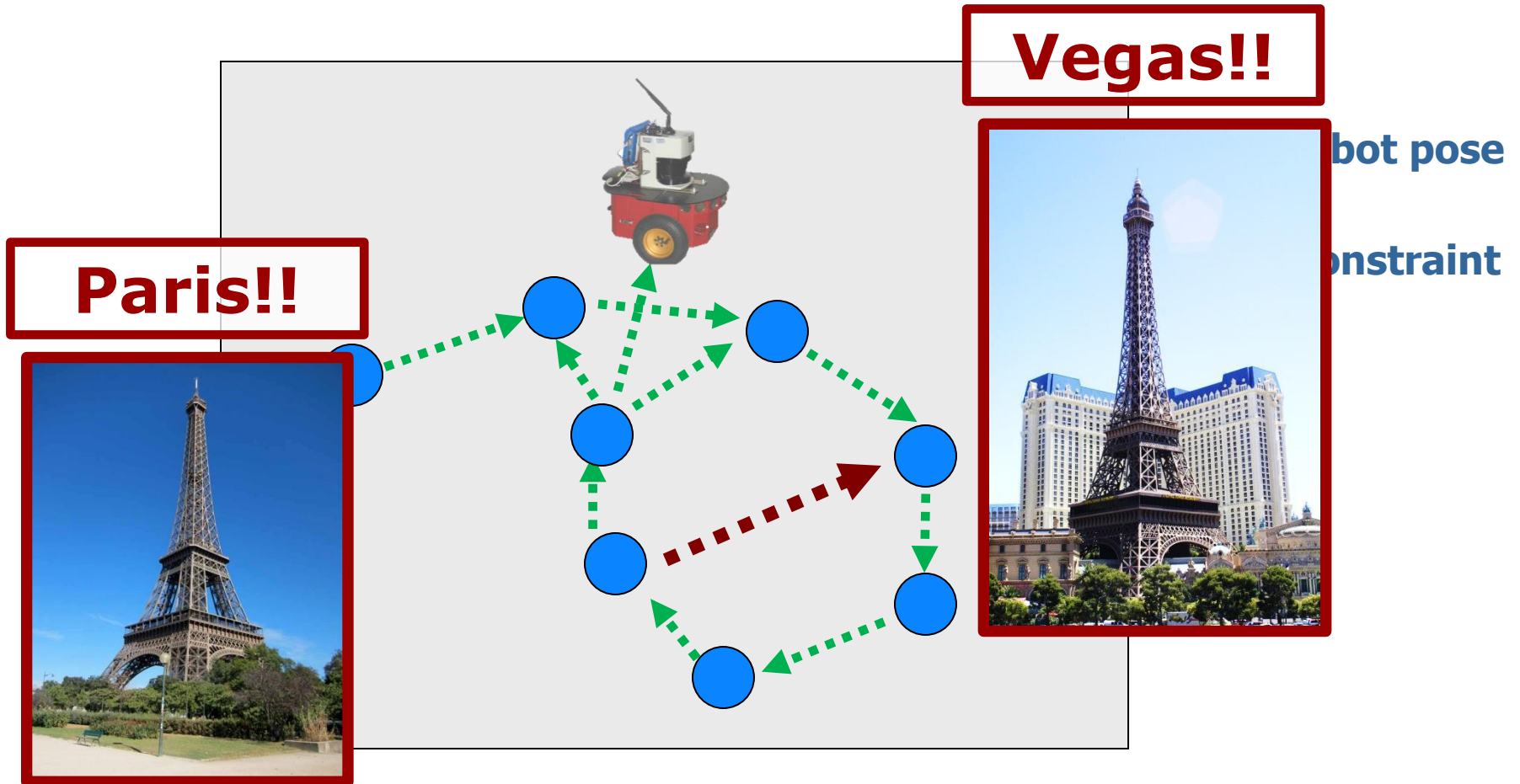
a single outlier ...

Graph-based SLAM



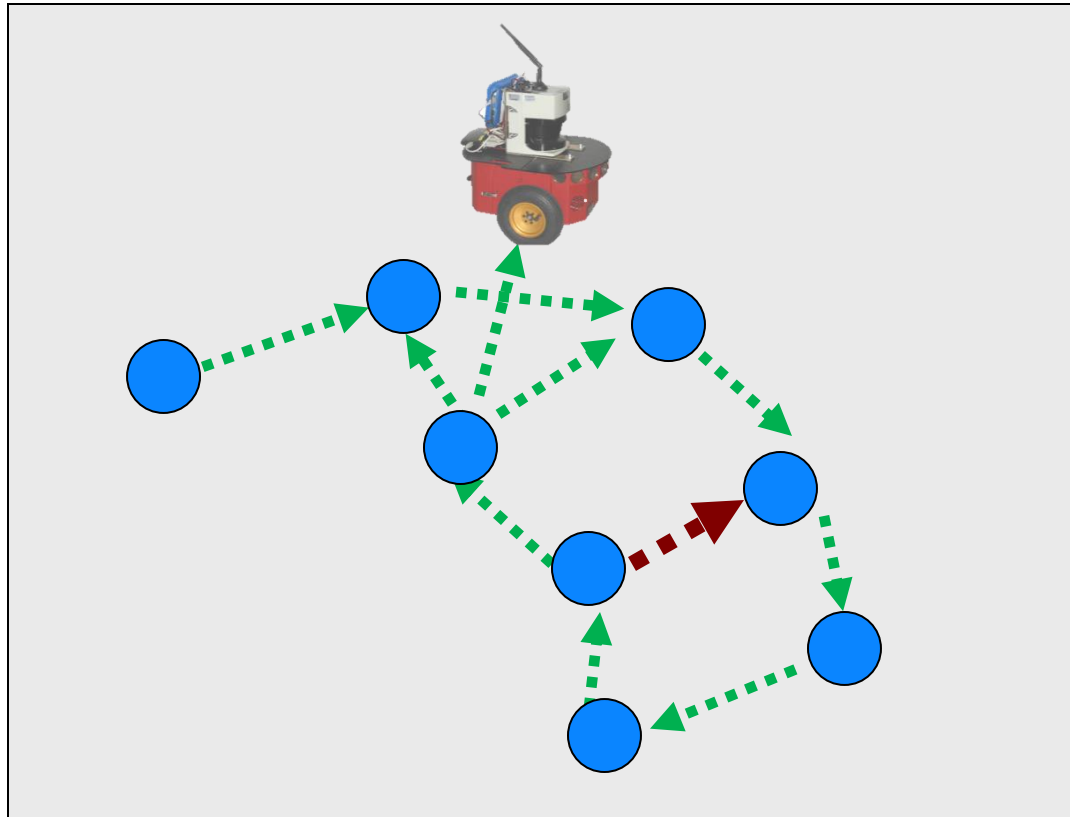
a single outlier ...

Graph-based SLAM



a single outlier ...

Graph-based SLAM



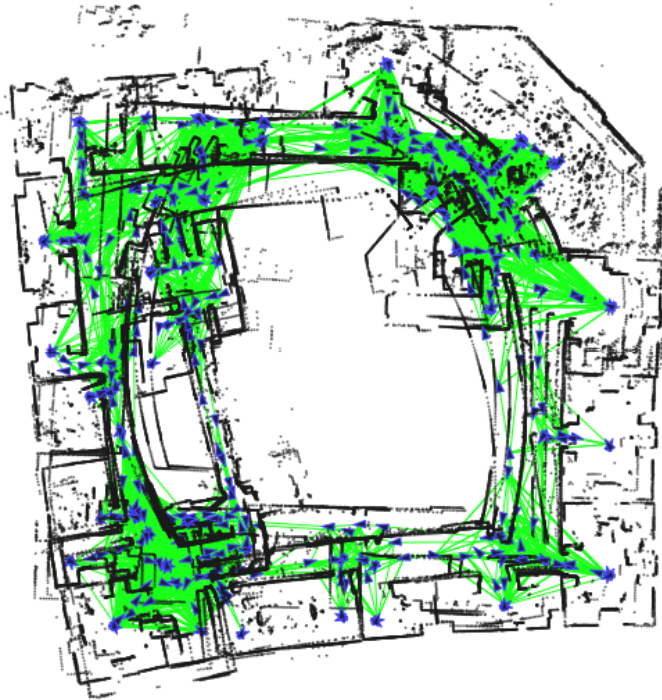
● Robot pose

→ Constraint

a single outlier ... ruins the map

Graph-SLAM Pipeline

Front end  Validation  Back end



Assumption:



**No
Outliers**

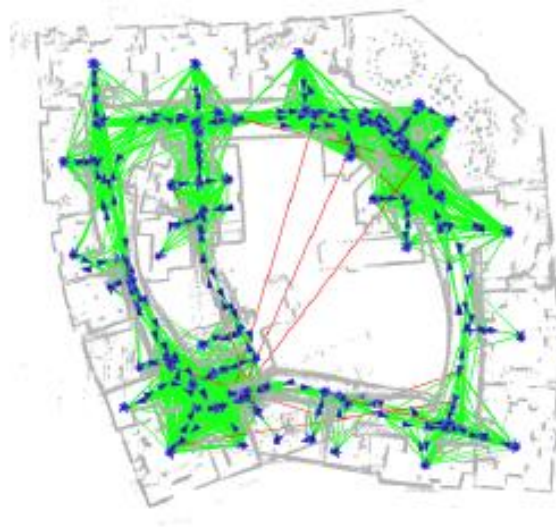


Impossible to have perfect validation

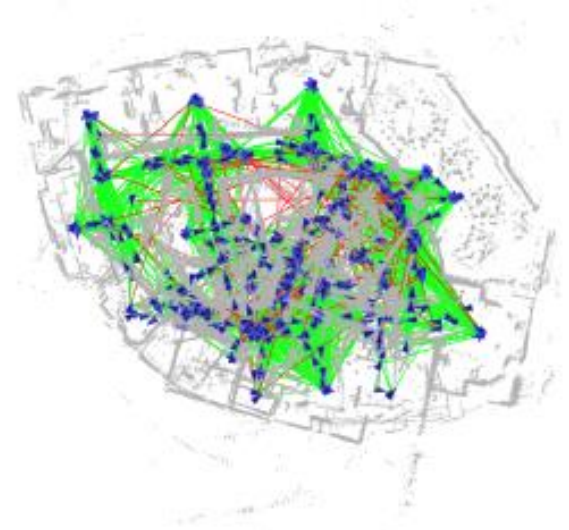
SLAM Back End Fails in the Presence of Outliers



**1
Outlier**

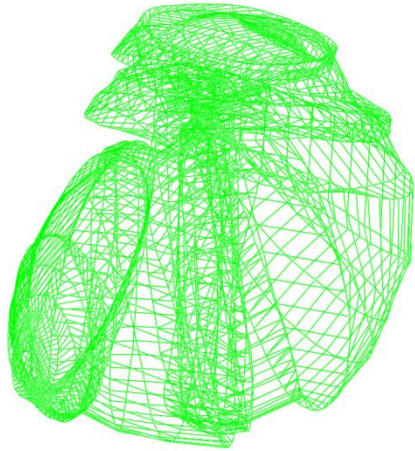


**10
Outliers**



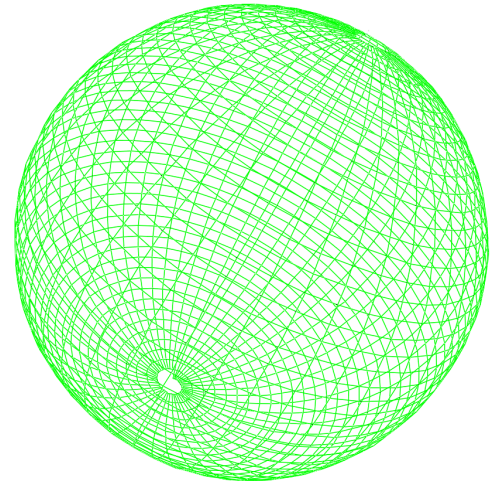
**100
Outliers**

SLAM Back End Depends on the Initial Guess

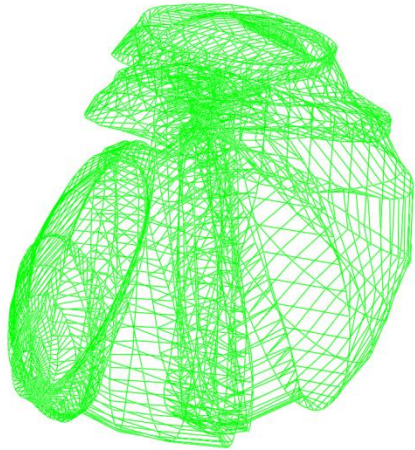


Good

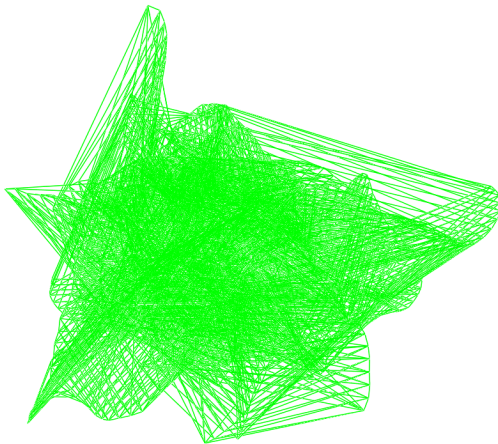
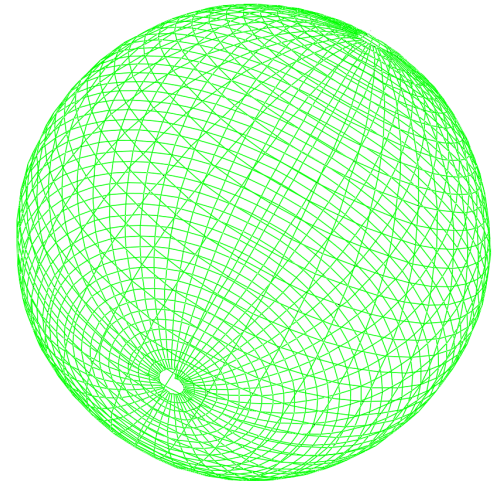
**Initial
Guess**



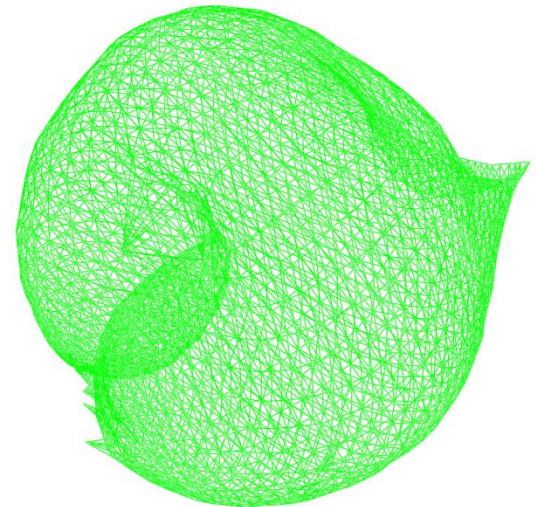
SLAM Back End Depends on the Initial Guess



Good
➔
**Initial
Guess**



Bad
➔
**Initial
Guess**



Typical Assumptions

- **Gaussian assumption is violated**
 - Perceptual aliasing
 - Measurement error
 - Multipath GPS measurements

Typical Assumptions

- **Gaussian assumption is violated**
 - Perceptual aliasing
 - Measurement error
 - Multipath GPS measurements
- **Linear approximation is invalid**
 - Linearization is only valid if close to optimum

Typical Assumptions in Graph-SLAM

- **No outliers**
- **Good initial guess**
- Current methods both **independently**
- Our method approaches **both problems**

Typical Assumptions in Graph-SLAM

- **No outliers**
- **Good initial guess**
- Current methods solve both **independently**
- Our method approaches **both problems**

Our Approach

- **Dynamic Covariance Scaling**

Our Approach: Dynamic Covariance Scaling


- Successfully **rejects** outliers
- More robust to **bad initial guess**
- Does not increase state space
- Is a robust M-estimator

Standard Gaussian Least Squares


$$X^* = \operatorname{argmin}_X \sum_{ij} \underbrace{\mathbf{e}_{ij}(X)^T \Omega_{ij} \mathbf{e}_{ij}(X)}_{\chi_{ij}^2}$$

Dynamic Covariance Scaling


$$X^* = \operatorname{argmin}_X \sum_{ij} \underbrace{\mathbf{e}_{ij}(X)^T \Omega_{ij} \mathbf{e}_{ij}(X)}_{\chi_{ij}^2}$$

$$X^* = \operatorname{argmin}_X \sum_{ij} \mathbf{e}_{ij}(X)^T (s_{ij}^2 \Omega_{ij}) \mathbf{e}_{ij}(X)$$


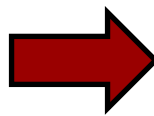
How to Determine s ?

$$X^* = \operatorname{argmin}_X \sum_{ij} \mathbf{e}_{ij}(X)^T (s_{ij}^2 \Omega_{ij}) \mathbf{e}_{ij}(X)$$


How to Determine s ?

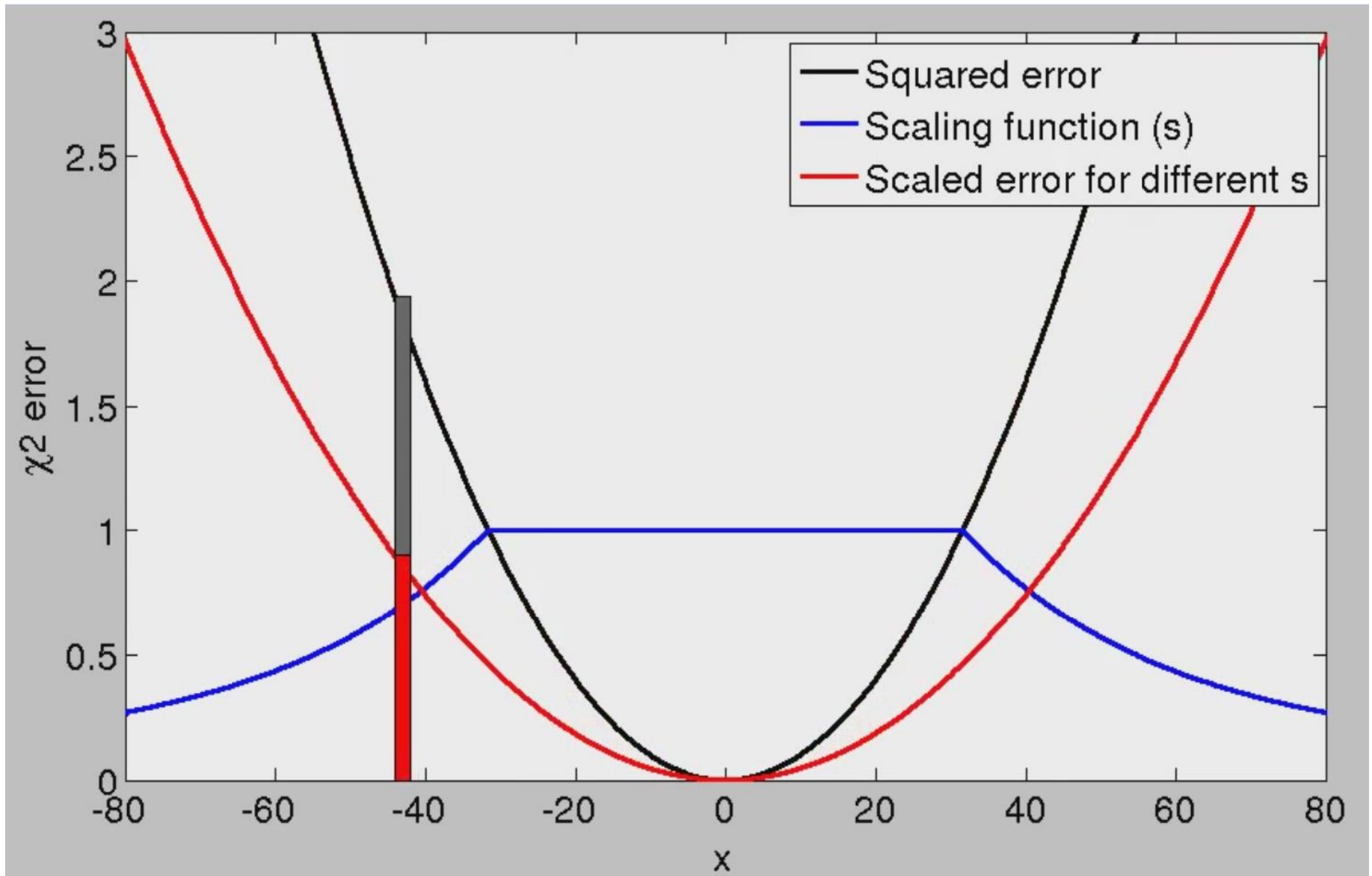
$$X^* = \operatorname{argmin}_X \sum_{ij} \mathbf{e}_{ij}(X)^T \left(s_{ij}^2 \Omega_{ij} \right) \mathbf{e}_{ij}(X)$$


⋮

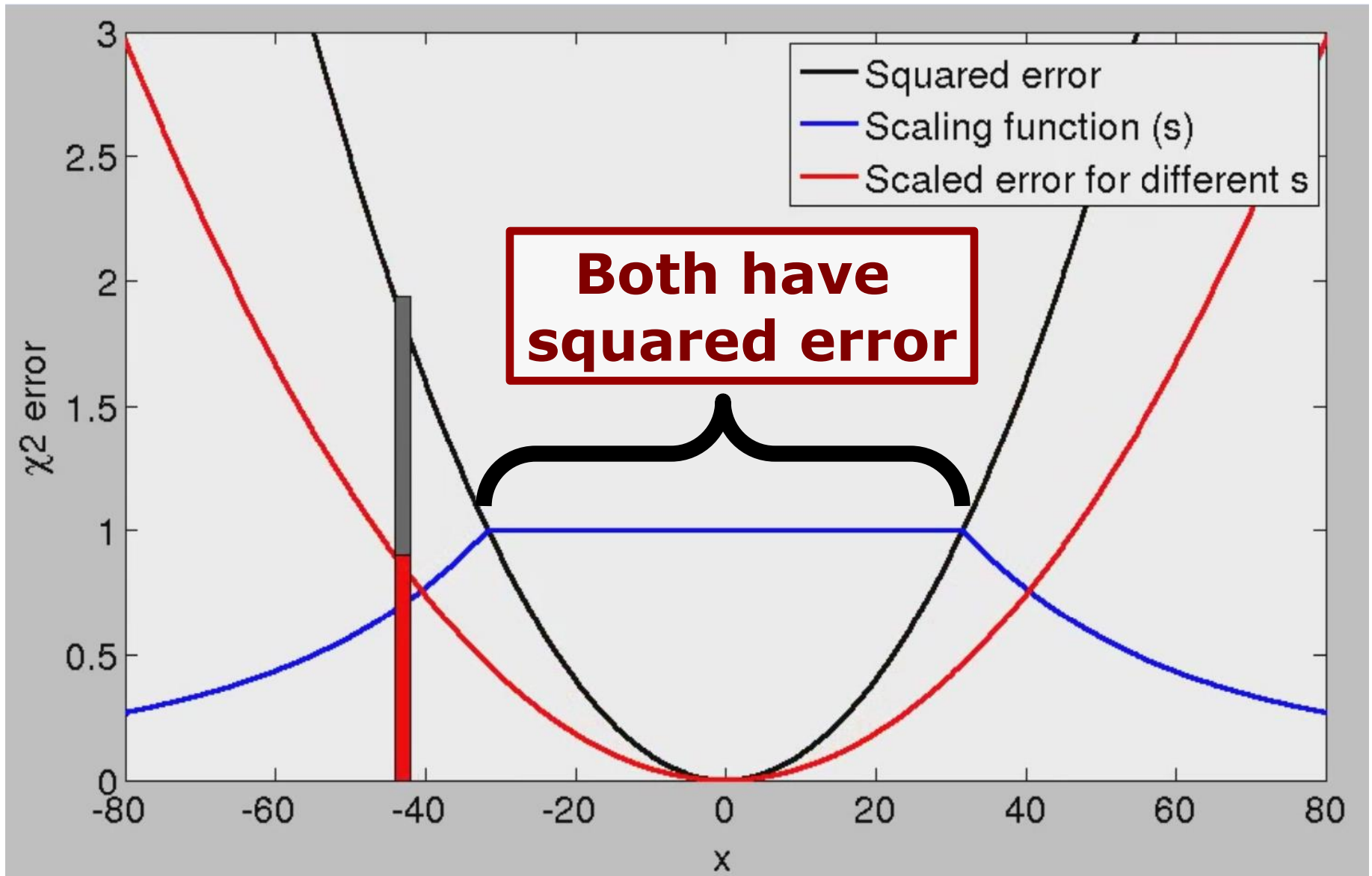

$$s_{ij} = \min \left(1, \frac{2\Phi}{\Phi + \chi_{ij}^2} \right)$$

Closed form approximation of Switchable Constraints with a M-estimator

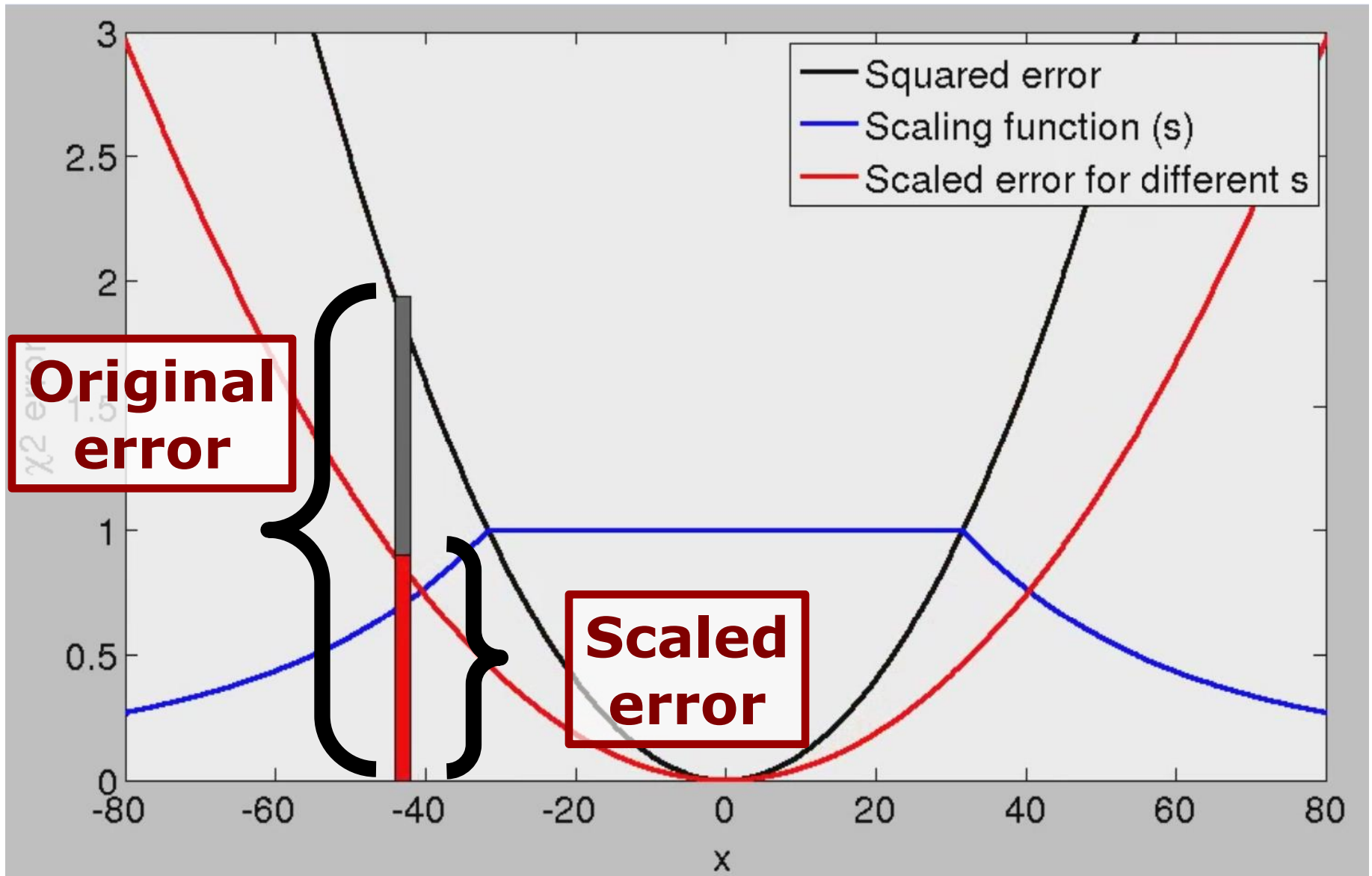
Dynamic Covariance Scaling



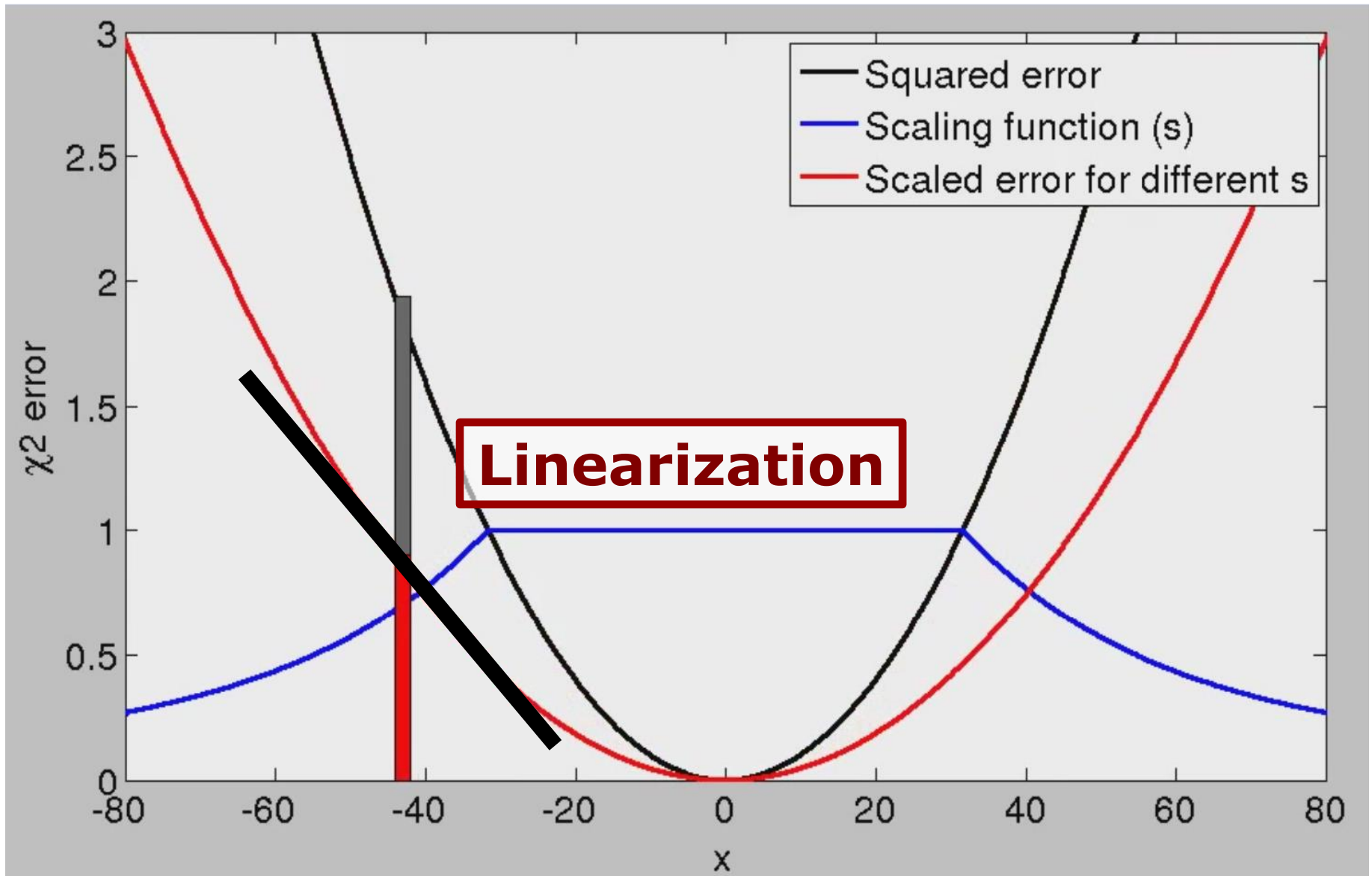
Dynamic Covariance Scaling



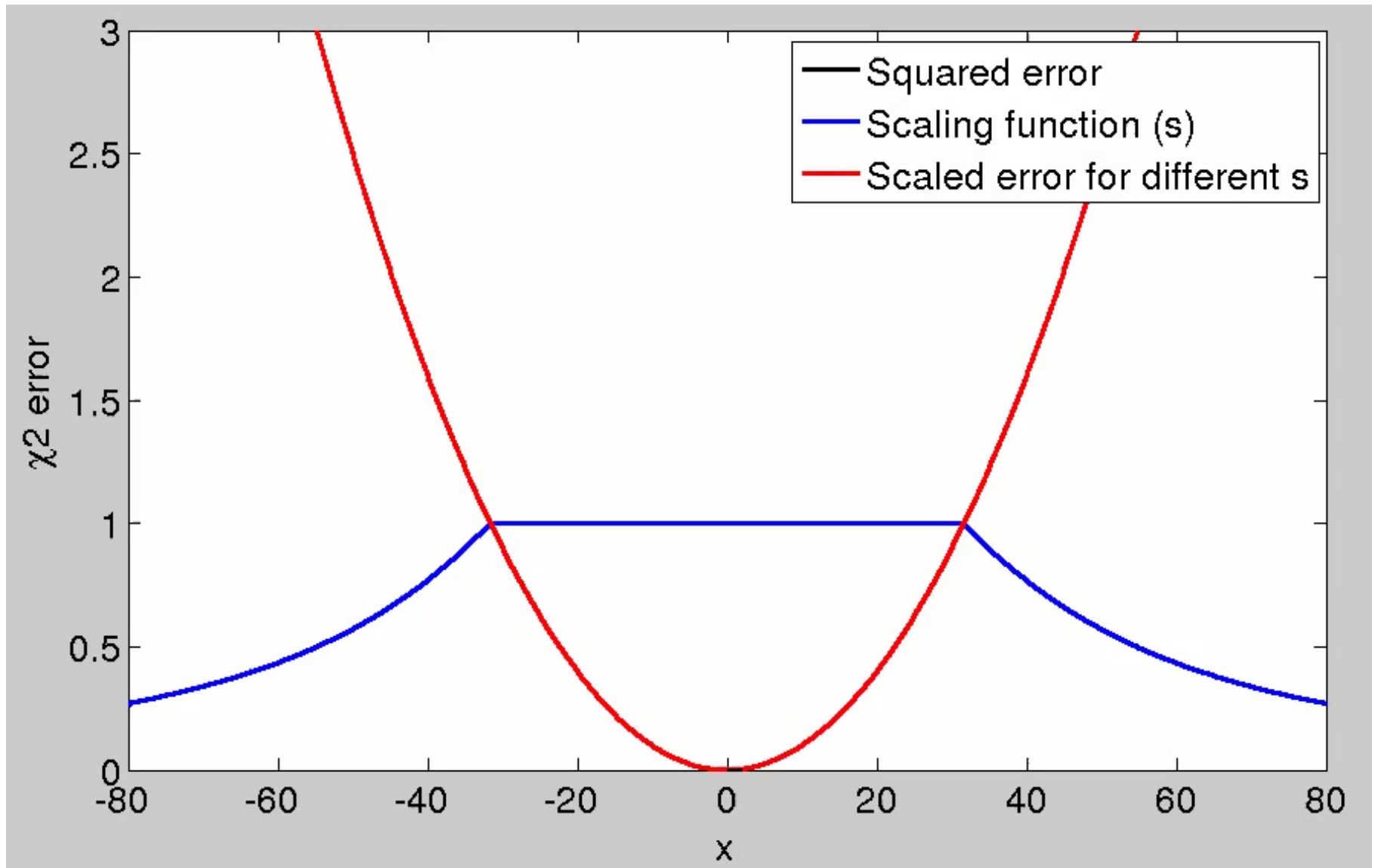
Dynamic Covariance Scaling



Dynamic Covariance Scaling



Dynamic Covariance Scaling



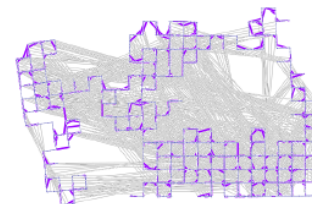
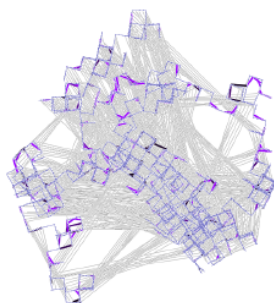
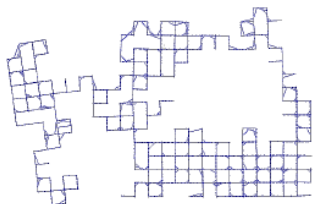
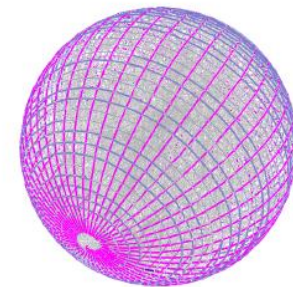
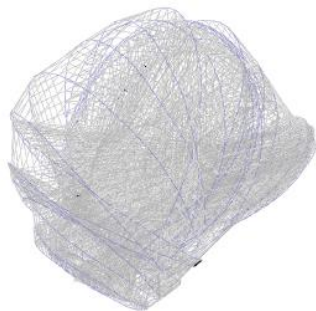
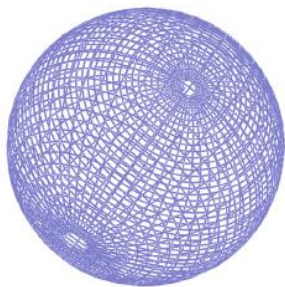
Robust SLAM with Our Method

Ground
Truth

Initialization

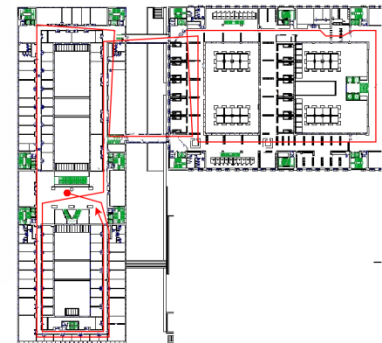
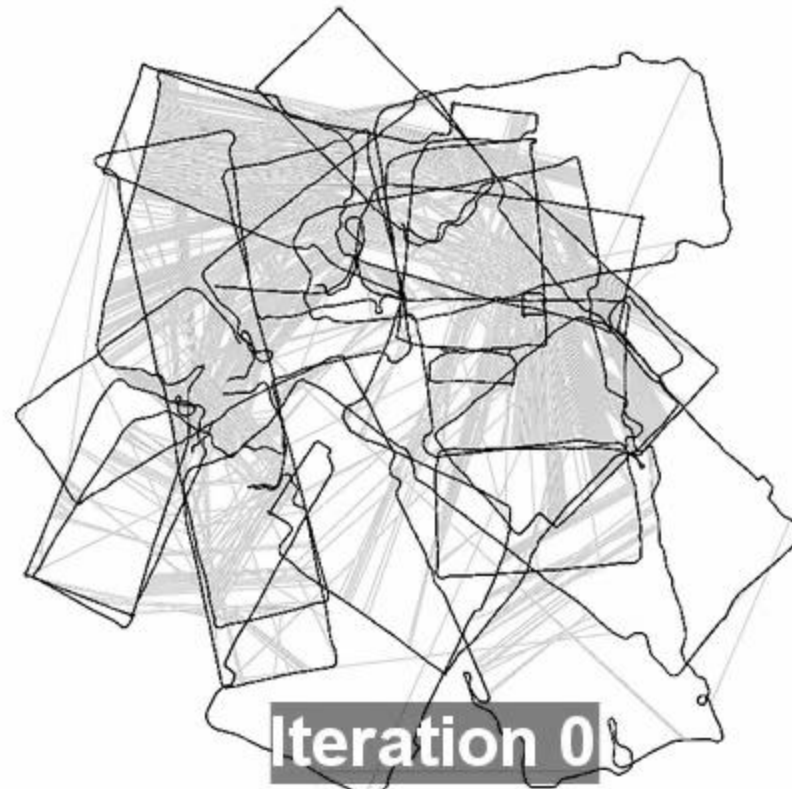
Gauss
Newton

**Our
Method**



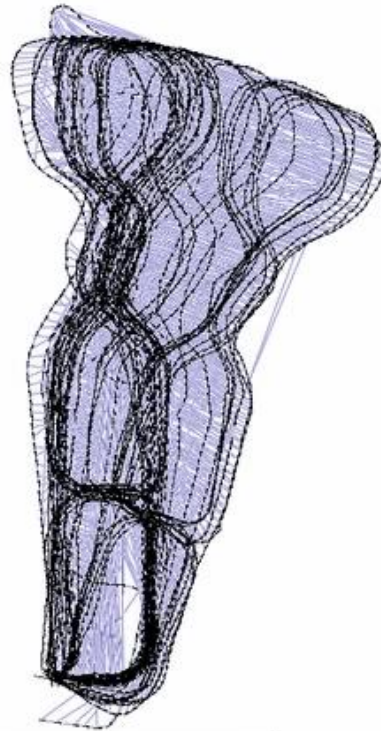
Manhattan3500 (1000 Outliers)
Sphere2500 (1000 Outliers)

Dynamic Covariance Scaling with Front-end Outliers



Bicocca multiseession dataset

Dynamic Covariance Scaling with Front-end Outliers

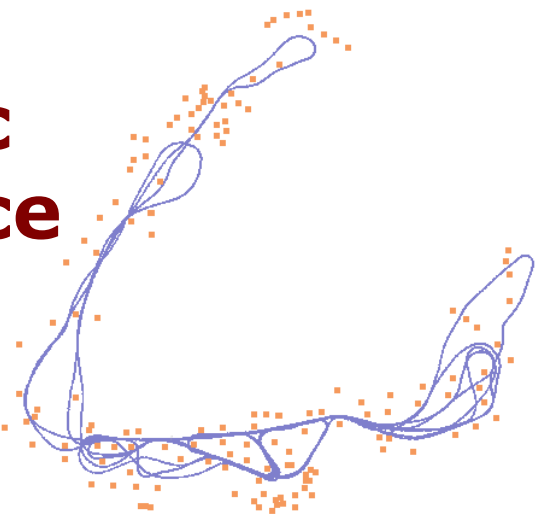


Iteration 0

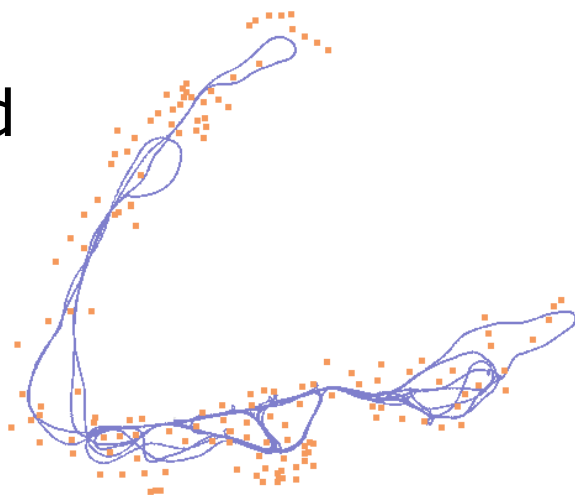
Lincoln-labs multisession dataset

Robust SLAM with Our Method

**Dynamic
Covariance
Scaling**



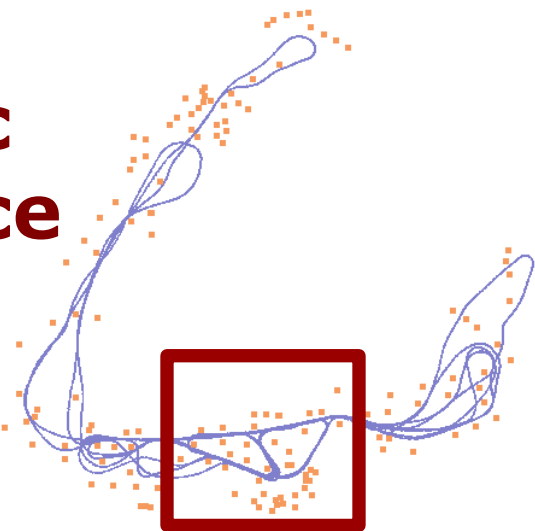
Standard
Gauss-
Newton



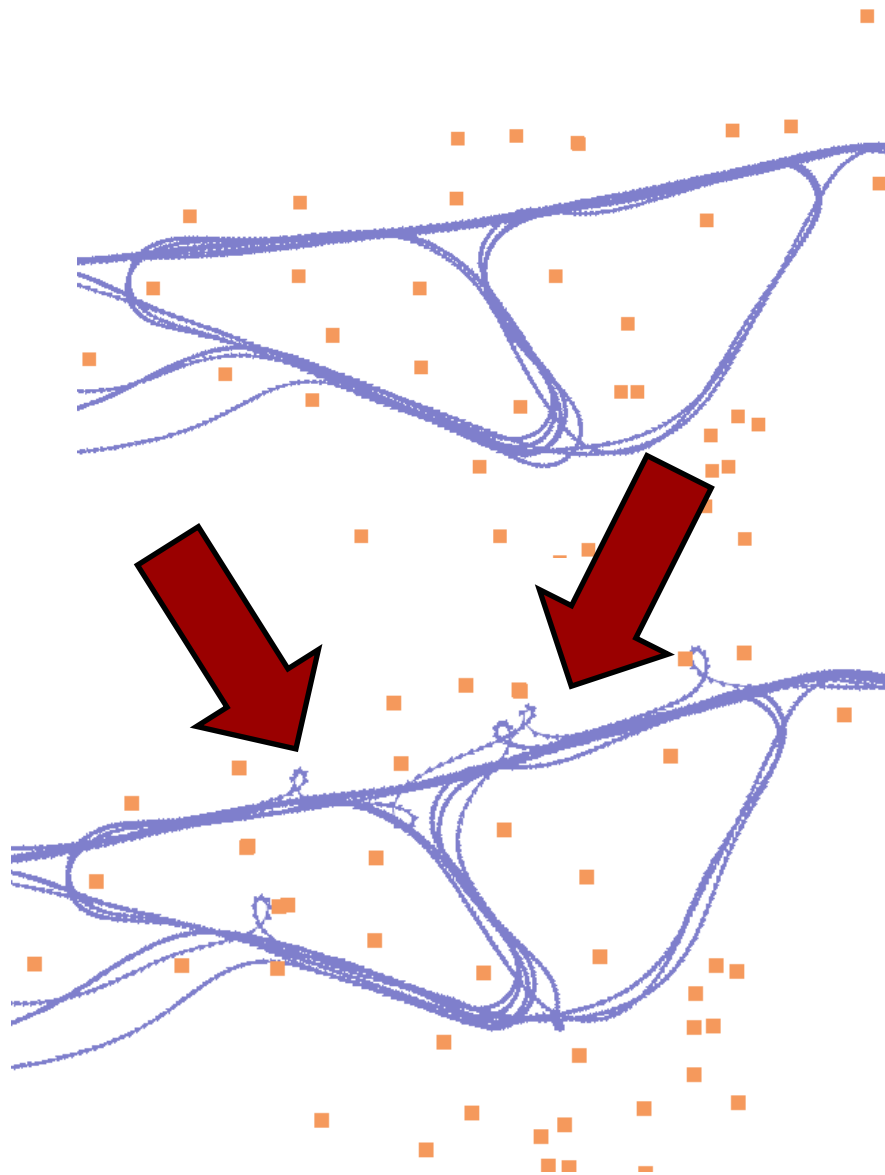
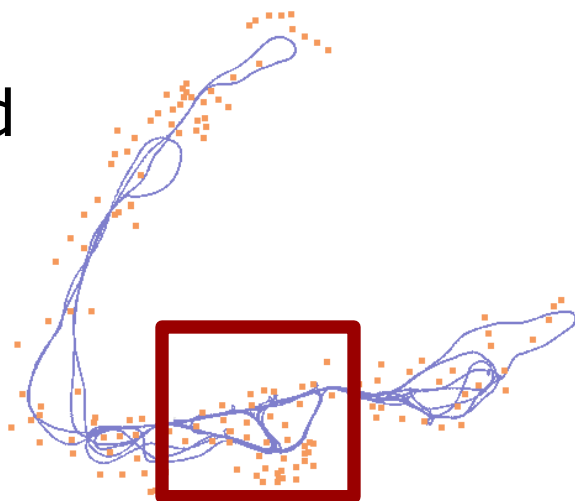
Victoria Park
Initialization
(Odometry)

Robust SLAM with Our Method

**Dynamic
Covariance
Scaling**

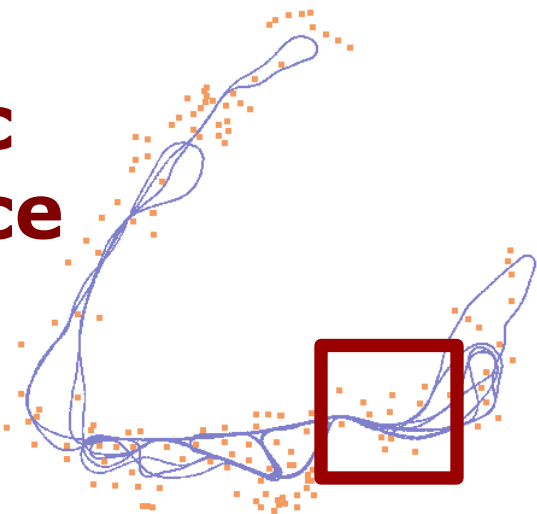


Standard
Gauss-
Newton

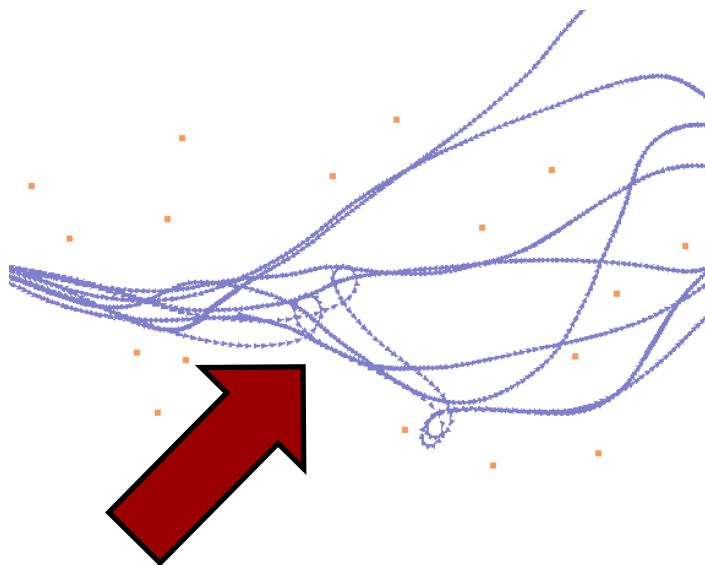
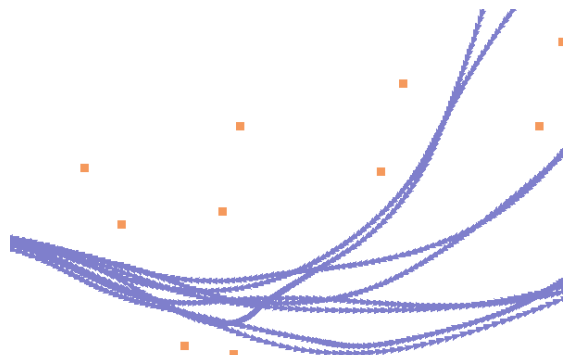
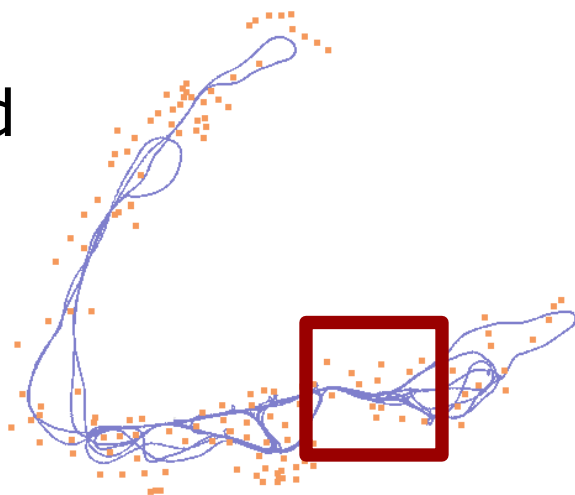


Robust SLAM with Our Method

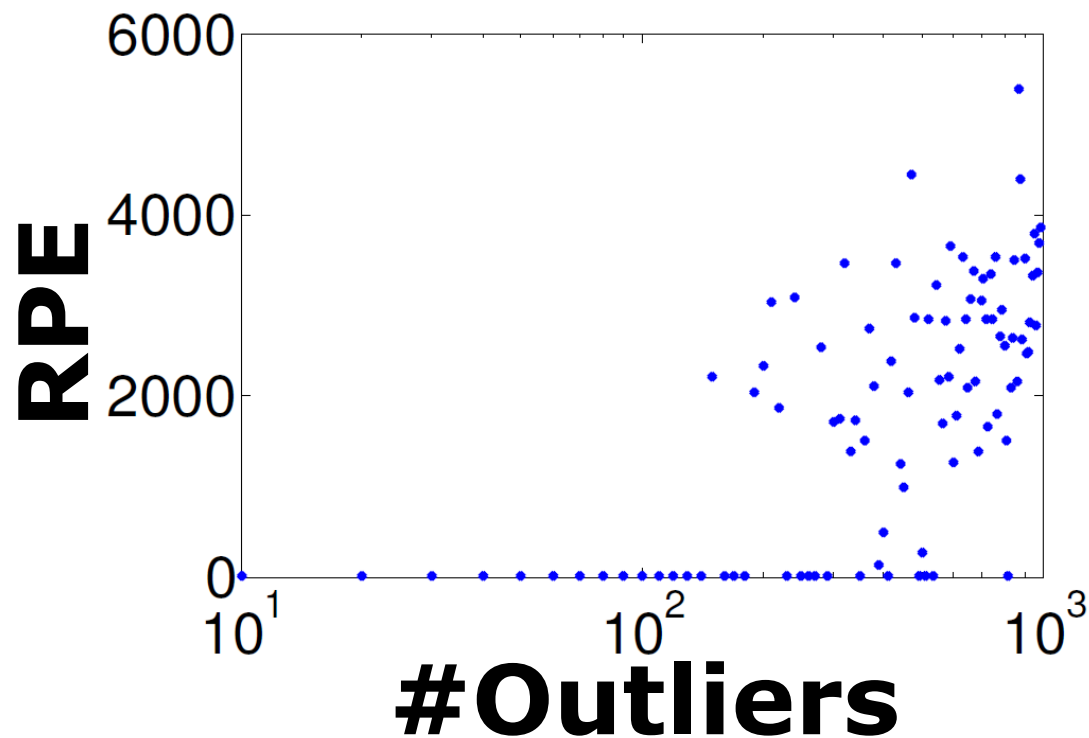
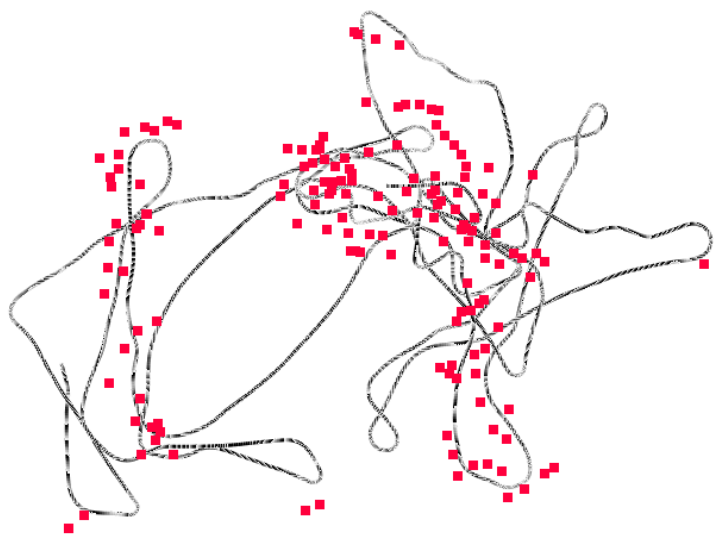
**Dynamic
Covariance
Scaling**



Standard
Gauss-
Newton



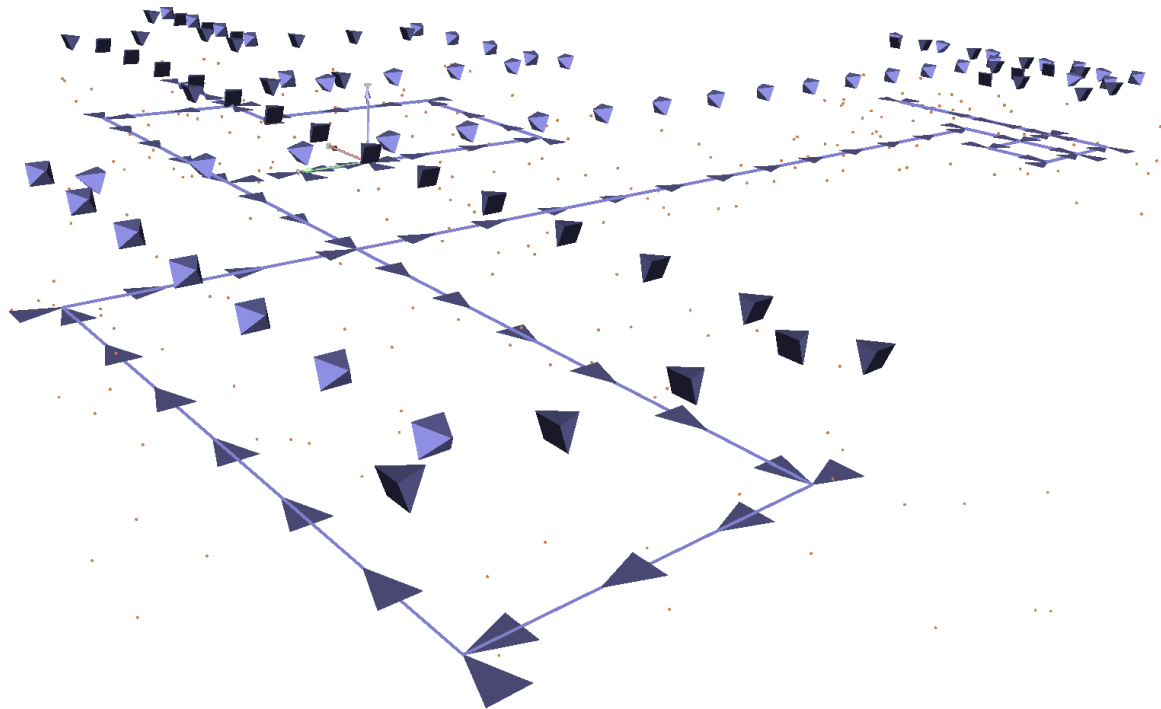
Dynamic Covariance Scaling with Outliers in Victoria Park



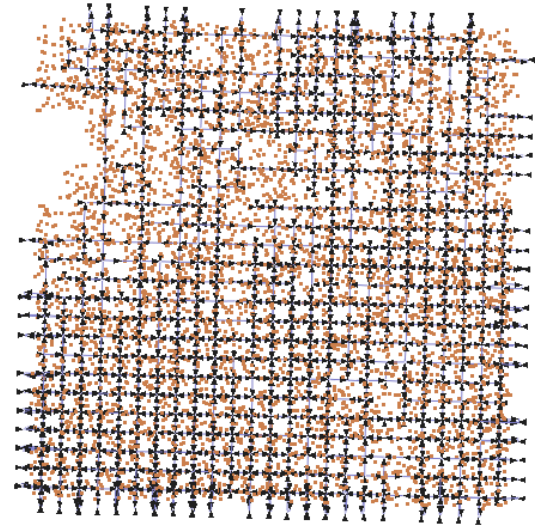
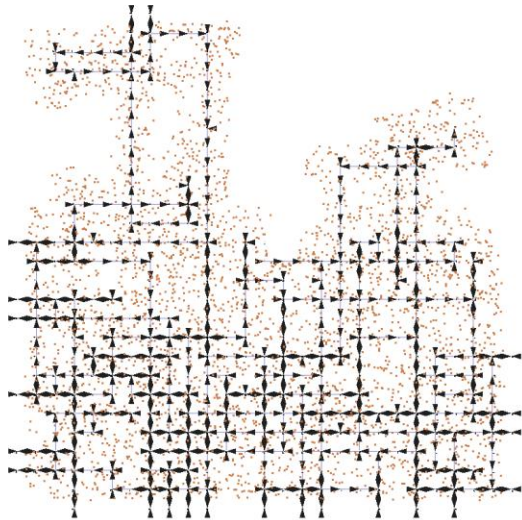
- DCS recovers correct solution
- GN fails to converge to the correct solution even for **outlier-free case**

Robust Visual SLAM with Our Method

- 3D grid worlds of different sizes
- Robot perceives point landmarks



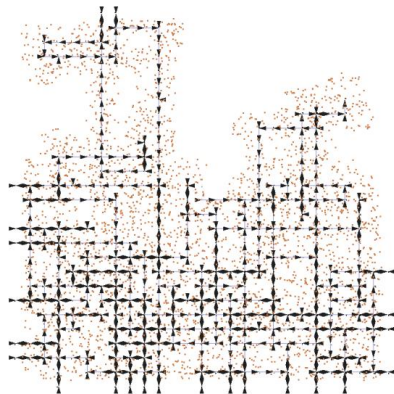
Robust Visual SLAM with Our Method



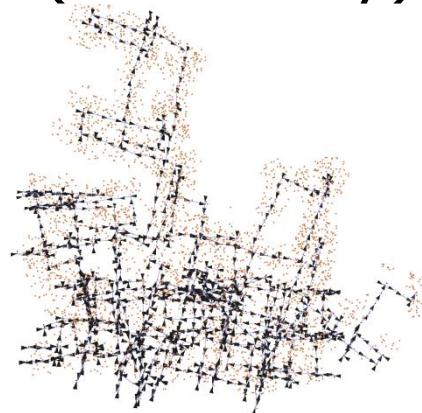
- ~ 1000 camera poses
- ~ 4000 features
- $\sim 20\text{K}$ constraints
- ~ 5000 camera poses
- ~ 5000 features
- $\sim 100\text{K}$ constraints

Robust Visual SLAM with DCS

Ground
Truth



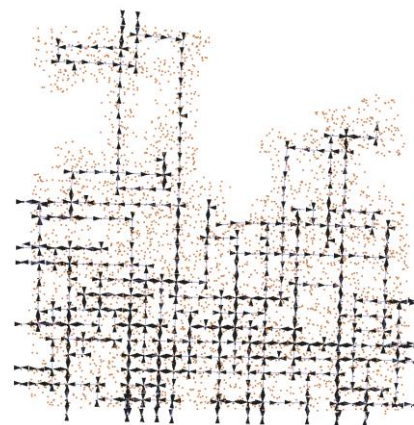
Initialization
(Odometry)



Simulated Stereo
(Bad initial guess)



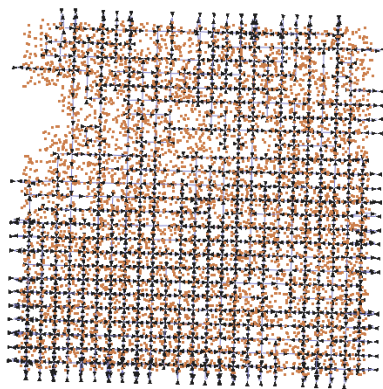
Levenberg-Marquardt
(100 iterations)



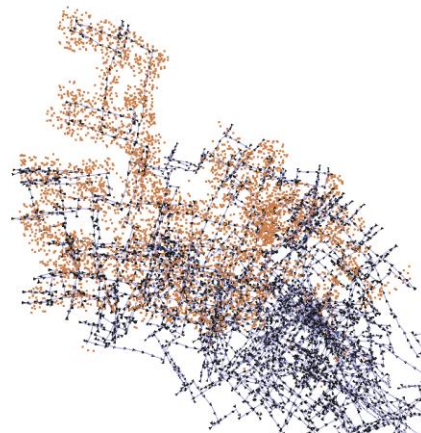
Our Method
(15 iterations)

Robust Visual SLAM with DCS

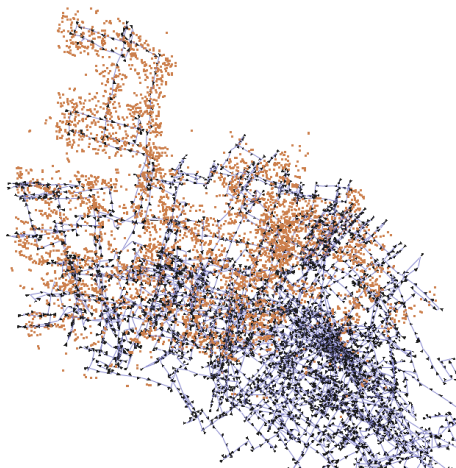
Ground
Truth



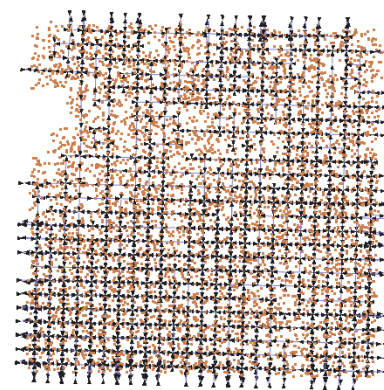
Initialization
(Odometry)



Simulated Stereo
(Bad initial guess)

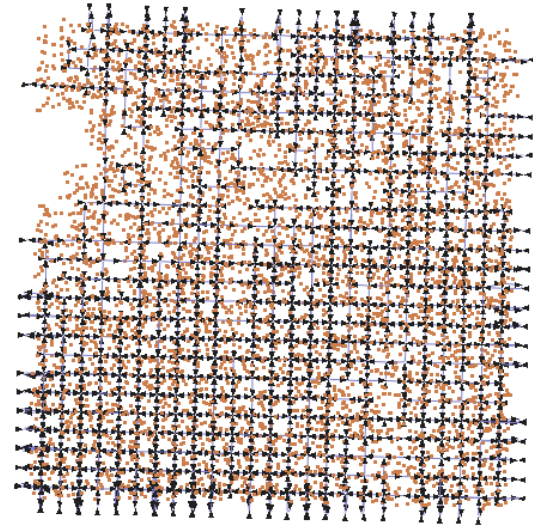
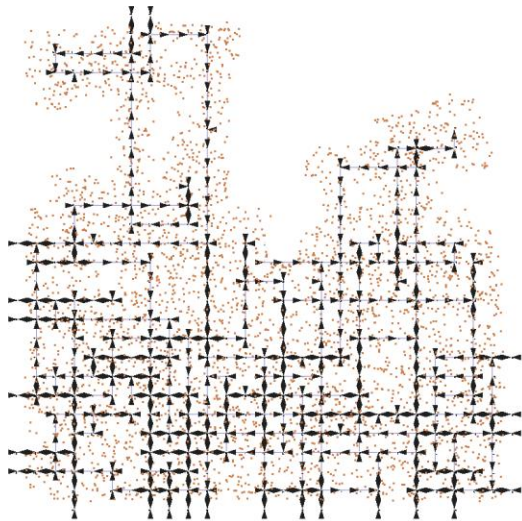


Levenberg-Marquardt
(150 iterations)



Our Method
(15 iterations)

Robust Visual SLAM with DCS



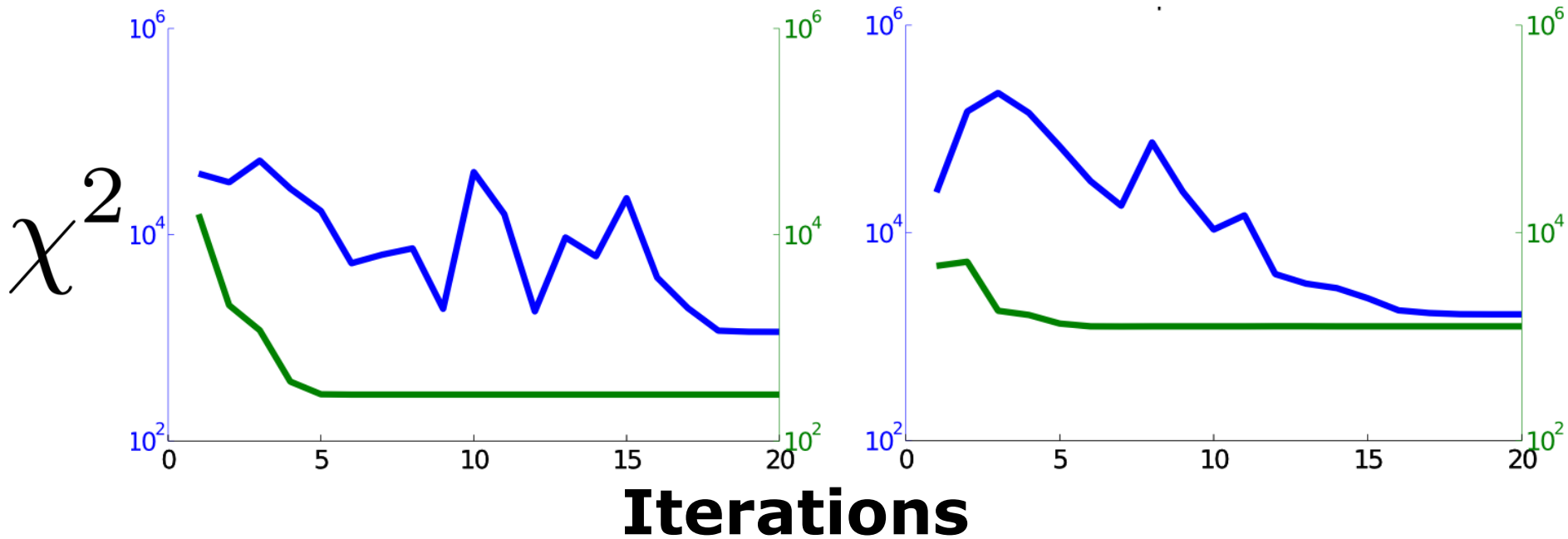
- DCS recovers correct solution in the presence of up to **25% outliers**
- LM fails to converge to the correct solution even for **outlier-free cases**

Convergence – 1000 Outliers

- **Switchable Constraints**
- **Dynamic Covariance Scaling**

Manhattan3500

Sphere2500



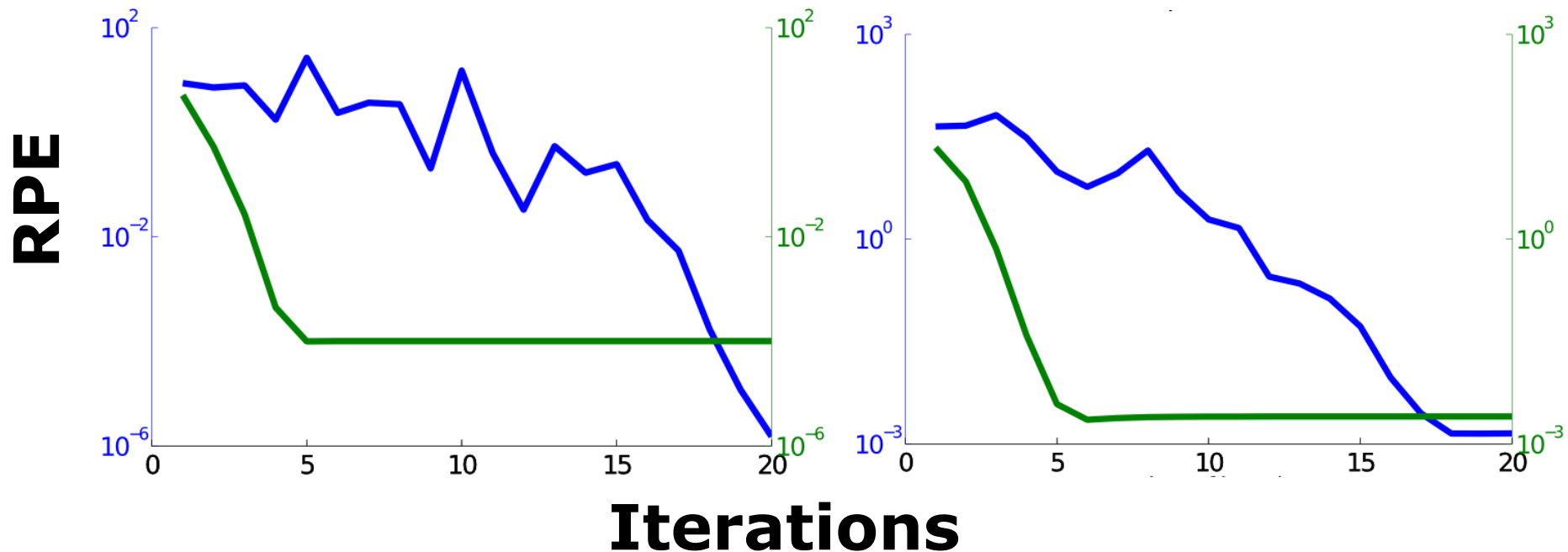
Convergence – 1000 Outliers

■ **Switchable Constraints**

■ **Dynamic Covariance Scaling**

Manhattan3500

Sphere2500



Convergence with Outliers

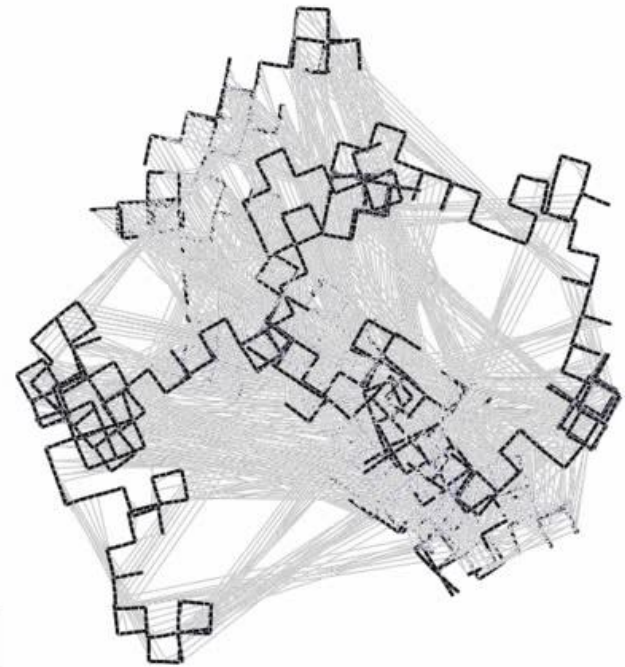
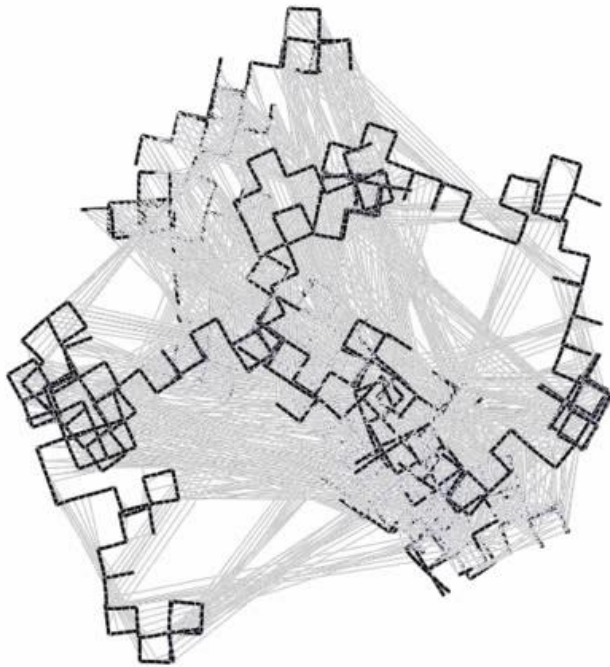
Switchable Constraints

Dynamic Covariance Scaling

Switchable Constraints (SC)

ManhattanOlson

Dynamic Covariance Scaling (DCS)



Iteration 0

Conclusion

- **Rejects outliers** for 2D & 3D SLAM
- **No increase in computational complexity**
- More robust to **bad initial guess**
- Now **integrated in g2o**

Thank you for your attention!